

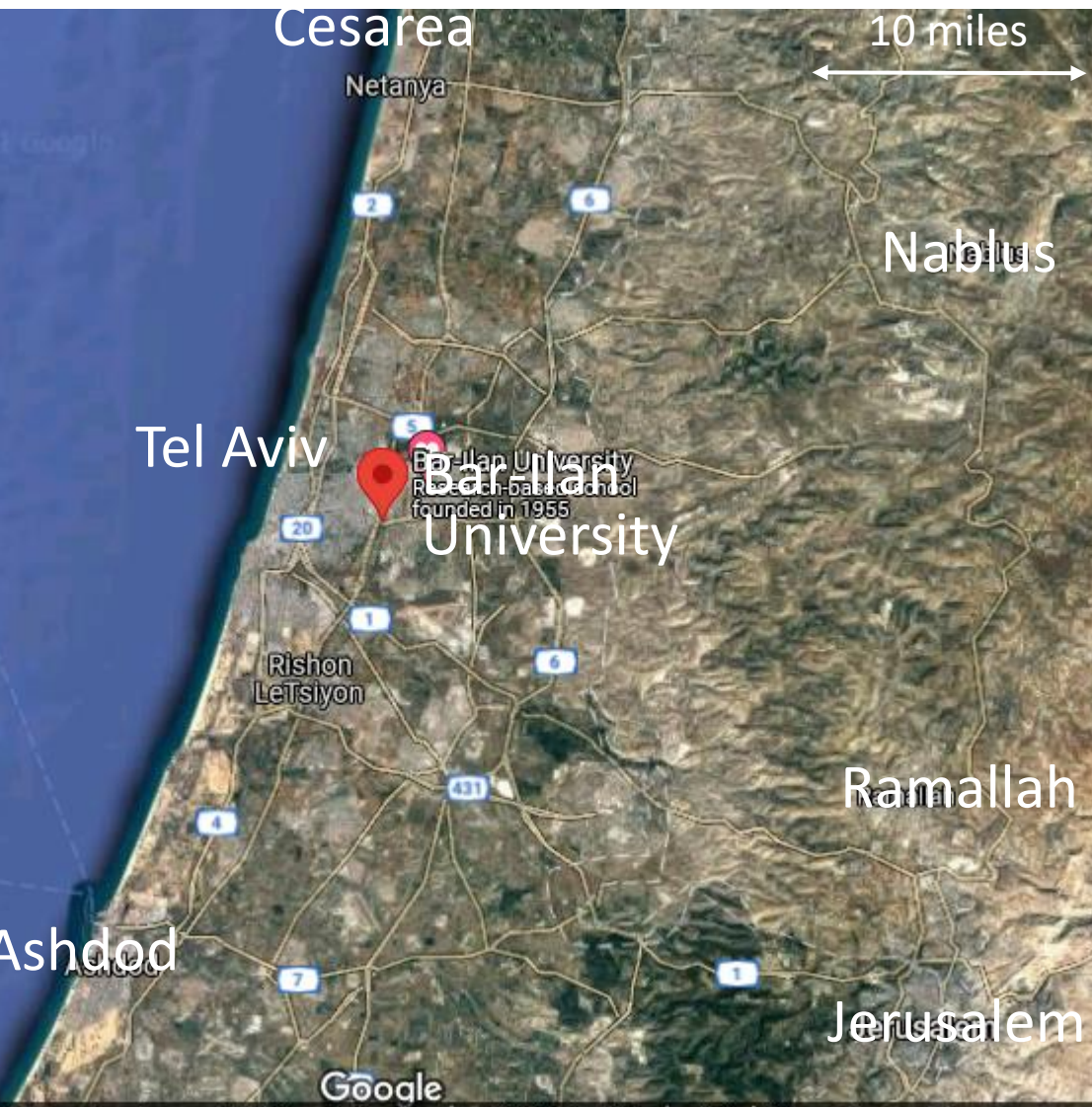
QIQT23 – June 1st, 2023

Quantum Simulations using quantum computers on the cloud

Emanuele Dalla Torre

Bar-Ilan University

Bar-Ilan University (established 1955)



20,000 students, 1350 faculty members

Dynamics of complex quantum systems



Eran Sela
Tel Aviv University



Sourin Das



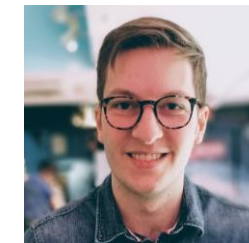
Sowrabh Sudevan
IISER Kolkata



Matthew
Reagor



Maxime
Dupont



Bram
Evert



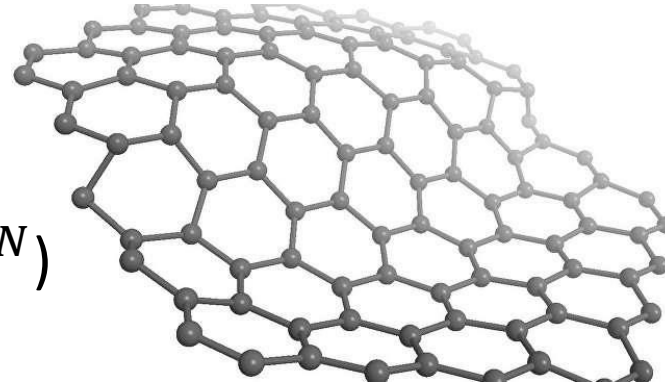
Atanu Rajak
BarIlan → Kolkata



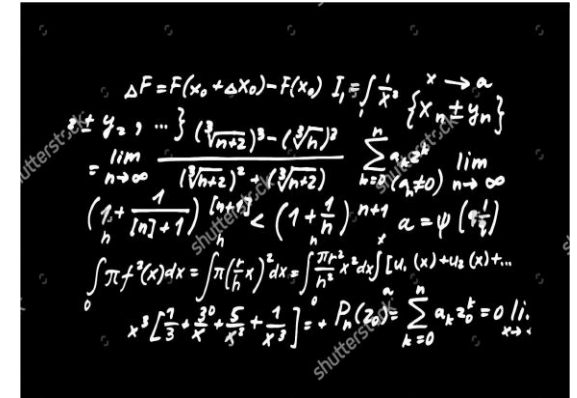
Quantum simulations

Quantum molecules/material

State vector: 2^N complex numbers
(instead of a single number of size 2^N)



Quantum field theories

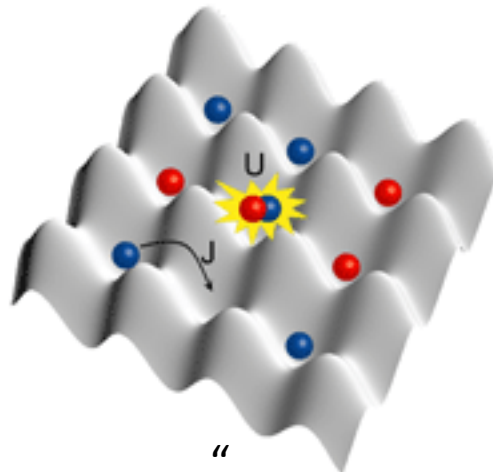

$$\Delta F = F(x_0 + \Delta x_0) - F(x_0) \quad I_1 = \int_{x_0}^{x_1} f(x) dx$$
$$= \lim_{n \rightarrow \infty} \frac{1}{n} \sum_{k=0}^{n-1} f\left(\frac{k}{n}\right) = \lim_{n \rightarrow \infty} \frac{1}{n} \sum_{k=0}^{n-1} f\left(\frac{k}{n}\right) = \lim_{n \rightarrow \infty} \frac{1}{n} \sum_{k=0}^{n-1} f\left(\frac{k}{n}\right)$$
$$\int \pi f^2(x) dx = \int \pi \left(\frac{f}{h}\right)^2 dx = \int \frac{\pi}{h^2} f^2 dx = \int \frac{\pi}{h^2} f^2 dx$$
$$x^2 \left[\frac{1}{3} + \frac{3}{x^2} + \frac{5}{x^4} + \frac{1}{x^6} \right] = P_n(x) = \sum_{k=0}^n a_k x^k = 0 \quad |i\rangle$$

Classical supercomputers



“If I try my best to make the equations look as near as possible to what would be imitable by a classical probabilistic computer, I get into trouble.” – Richard Feynman

Ultracold atoms



Quantum computer on the cloud



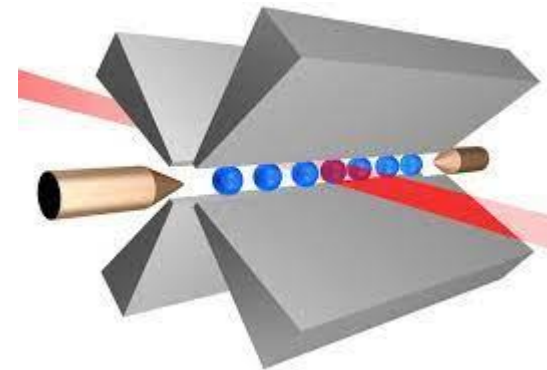
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Quantum computers - platforms

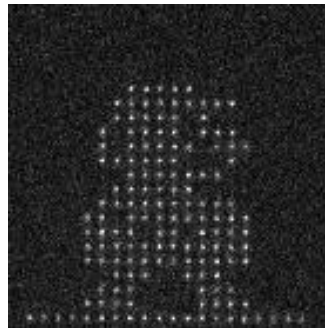
Superconducting circuits



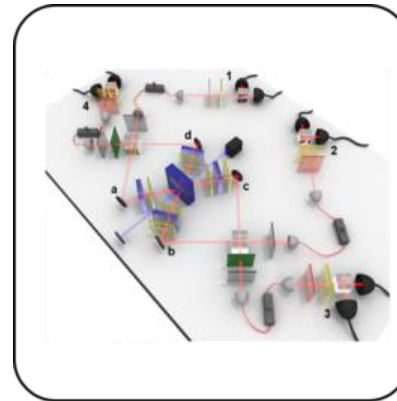
Trapped ions



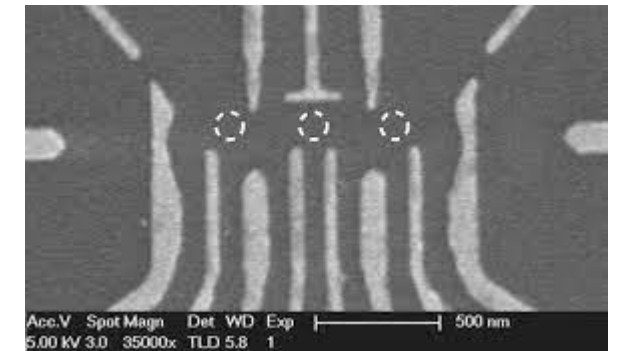
Rydberg atoms



Photons (MBQC)



Quantum wells (spin)



IQEra
COMPUTING INC.



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Quantum computers - platforms

1. **Neutral atoms** in optical lattices (qubit implemented by internal states of neutral atoms trapped in an optical lattice)
2. **Trapped ion** quantum computer (qubit implemented by the internal state of trapped ions)
3. **Superconducting** quantum computing (qubit implemented by the state of small superconducting circuits [Josephson junctions])
4. **Photonics** optical frequency photon as qubits, large entangled cluster state
5. **Silicon Spin** computer (qubit given by the spin states of trapped electrons in a transistor)
6. **Twistronics** – magic angle graphene layers allow for local control of Josephson junction qubits
7. **Optical Quantum Dot** computer – optically controlled spin qubit integrated with the light source
8. **NV Diamond-based** quantum computer (qubit realized by the electronic or nuclear spin of nitrogen-vacancy centers in diamond)
9. **Metallic-like carbon nanospheres** quantum computers (spins of itinerant electron within these nanospheres)
10. **Electrons-on-helium** quantum computers (qubit is the electron spin)
11. **Spatial-based Quantum Dot computer** (qubit given by electron position in double quantum dot)
12. **Engineered quantum wells** quantum computing, which could in principle enable the construction of quantum computers that operate at room temperature
13. **Coupled quantum wire** (qubit implemented by a pair of quantum wires coupled by a quantum point contact)
14. **Nuclear magnetic resonance** quantum computer (NMRQC) implemented with the nuclear magnetic resonance of molecules in solution, where qubits are provided by nuclear spins within the dissolved molecule and probed with radio waves
15. **Solid-state NMR** quantum computers (qubit realized by the nuclear spin state of phosphorus donors in silicon)
16. **Cavity quantum electrodynamics** (CQED) (qubit provided by the internal state of trapped atoms coupled to high-finesse cavities)
17. **Molecular magnet** (qubit given by spin states)
18. **Fullerene-based ESR** quantum computer (qubit based on the electronic spin of atoms or molecules encased in fullerenes)
19. **Nonlinear optical** quantum computer (qubits realized by processing states of different modes of light through both linear and nonlinear elements)
20. **Linear optical** quantum computer (qubits realized by processing states of different modes of light through linear elements e.g. mirrors, beam splitters and phase shifters)
21. **Bose-Einstein condensate** quantum computer
22. **Transistor-based** quantum computer – string quantum computers with entrainment of positive holes using an electrostatic trap
23. **Rare-earth-metal-ion-doped inorganic crystal** quantum computers (qubit realized by the internal electronic state of dopants in optical fibers)
24. **Bound states of electrons localized in an array of nanowires**
25. **Point-defect spin qubits in engineered quantum wells**
26. **Electron spin qubits in graphene quantum dots or van der Waals heterostructures**
27. **Photonic quantum computation in a synthetic time dimension**
28. ...and more



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List by Serg Bell (Jacobs University) <https://arxiv.org/abs/2203.17181>

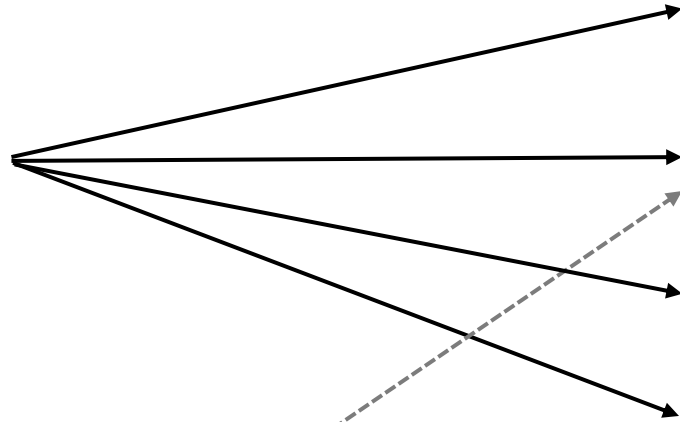
Quantum computing on the cloud: providers

IBM



IBM

amazon

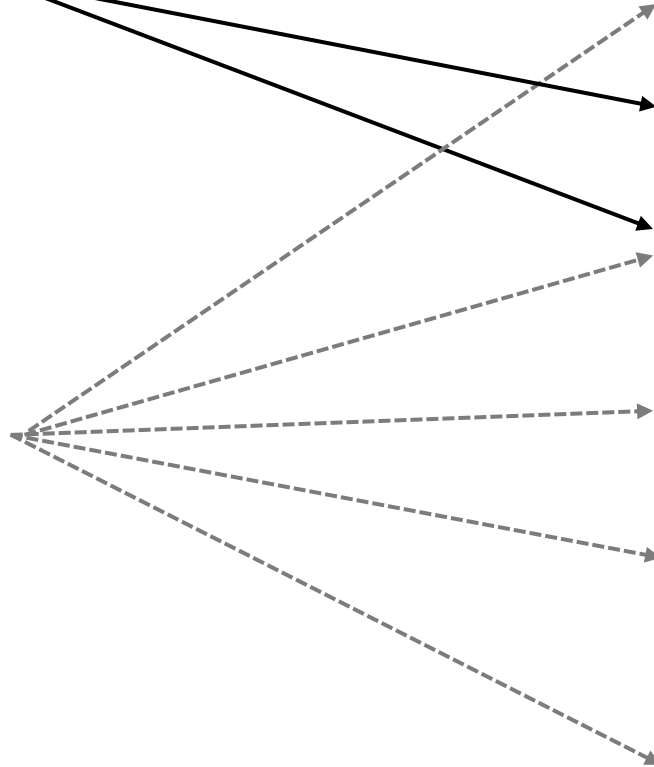


D-WAVE

rigetti

OQC

Microsoft



QuEra

IONQ

Honeywell

PASQAL

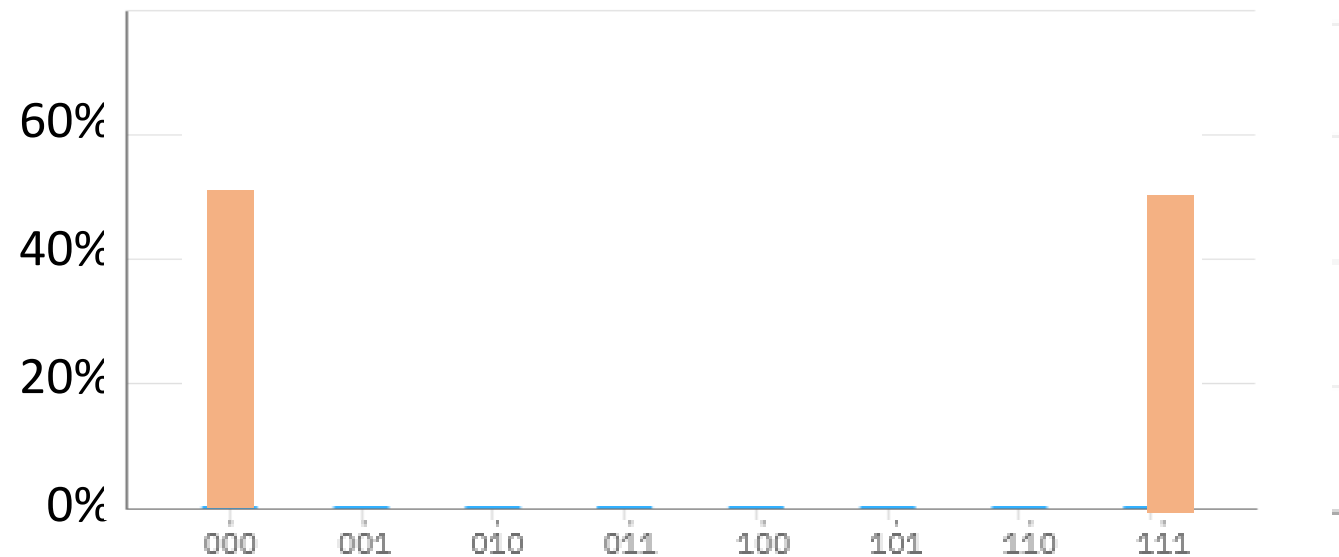
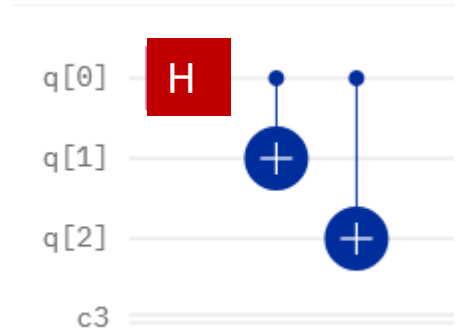


Quantum computers on the cloud: example

IBM quantum experience (qiskit)

<http://quantum-computing.ibm.com>

$$|\psi\rangle = \frac{1}{\sqrt{2}} (|000\rangle + |111\rangle)$$



ibmq_jakarta (13/09/2022)



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Noise and errors

ibmq_jakarta

Details

7

Qubits

16

Quantum
Volume

Status: ● Online

Total pending jobs: 3 jobs

Processor type ⓘ: Falcon r5.11H

Version: 1.0.16

Basis gates: CX, ID, RZ, SX, X

Your usage: 1866 jobs

Avg. CNOT Error: 7.874e-3

Avg. Readout Error: 2.959e-2

Avg. T1: 134.72 μ s

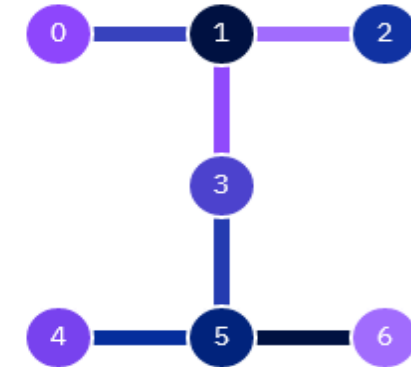
Avg. T2: 36.25 μ s

Providers with
access: 1 Providers ↓

Supports Qiskit
Runtime: Yes

1%

3%



My thumb rule: “sum the errors until you reach 50%”

Largest square circuit = 5 qubit X 5 gate



$$QV = 2^5 = 32$$



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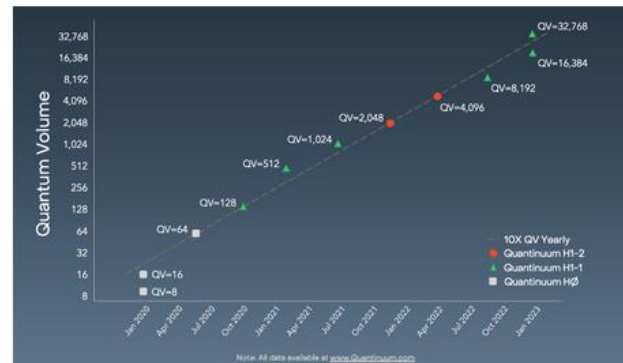
E. Pelofske, A. Bäertschi and S. Eidenbenz, "Quantum Volume in Practice: What Users Can Expect From NISQ Devices," in *IEEE Transactions on Quantum Engineering*, vol. 3, pp. 1-19, 2022, Art no. 3102119.



Quantum Volume reaches 5 digits for the first time: 5 perspectives on what it means for quantum computing

February 23, 2023

Quantinuum's H-Series team has hit the ground running in 2023, achieving a new performance milestone. The H1-1 trapped ion quantum computer has achieved a Quantum Volume (QV) of 32,768 (2^{15}), the highest in the industry to date.

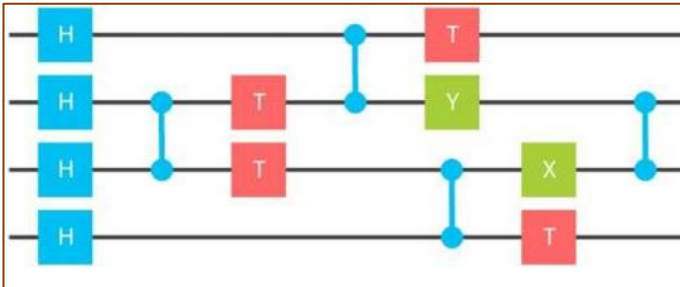


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The great challenge of quantum computing

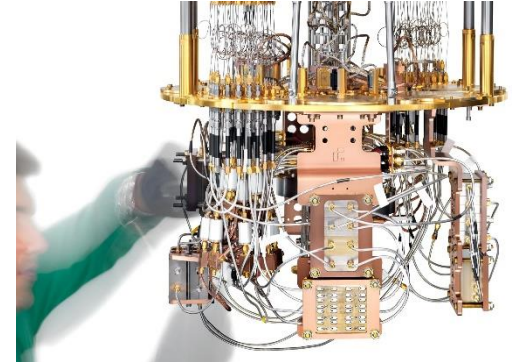
Model :

Unitary quantum computer



Reality :

Noisy superconducting circuits



Better hardware
Quantum error correction



Noisy models

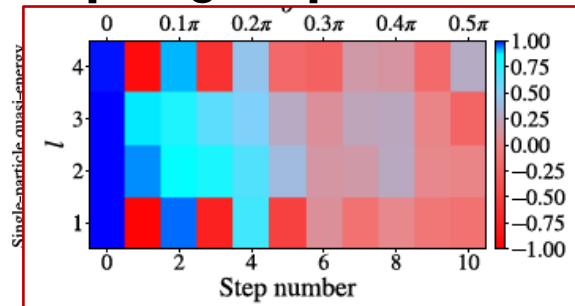


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Quantum simulations on quantum computers

Actual results on real hardware with up to 6 qubits

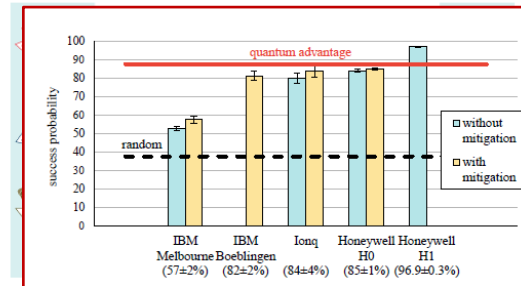
Topological phases in 1d



PRL 2020, PRB 2021



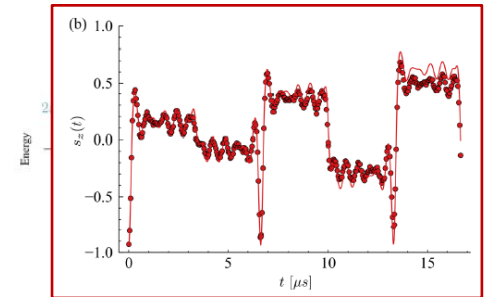
Nonlocal games



Adv Q Tech 2022



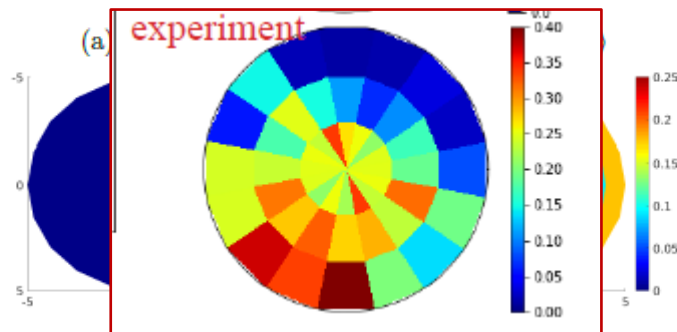
Long-range interactions



PRR 2021



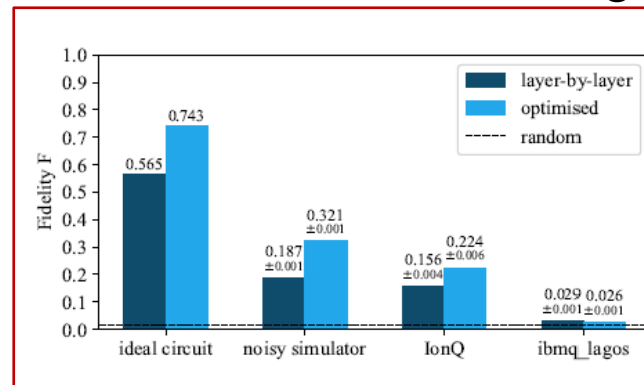
Bose-Einstein condensates



PRL 2022



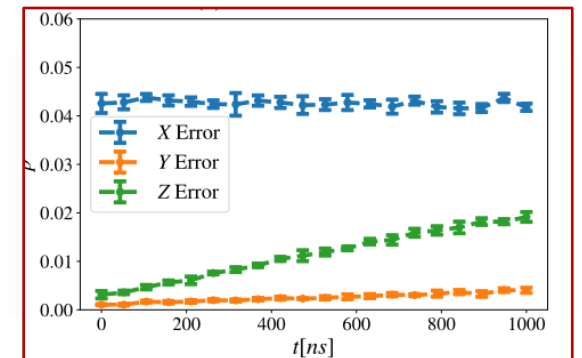
Quantum state encoding



arxiv



Quantum error detection

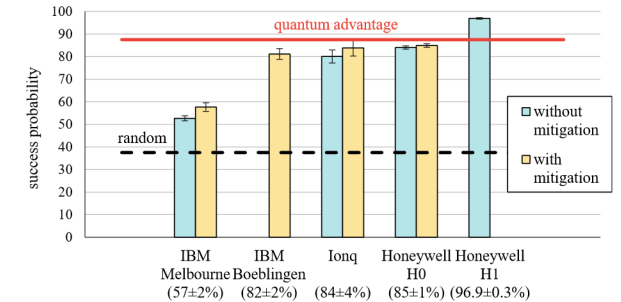


arXiv :2303.15508

What can you do with few qubits (and is it interesting?)

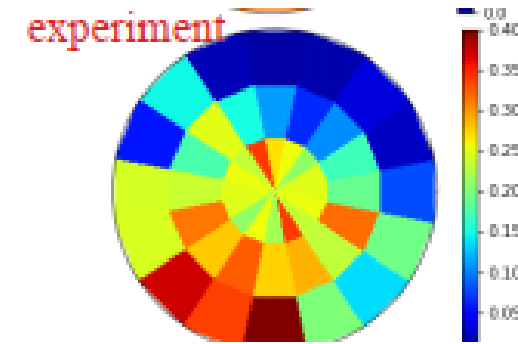
1) Non local games with 6 qubits

Sheffer, Azses, Dalla Torre, *Playing nonlocal games with 6 noisy qubits on the cloud*, *Adv. Quant. Tech* 2021



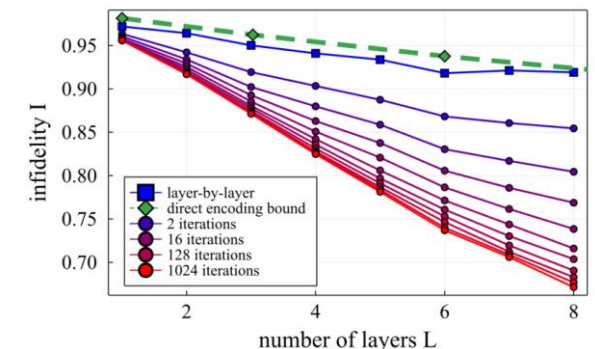
2) Simulating a BEC with 5 qubits

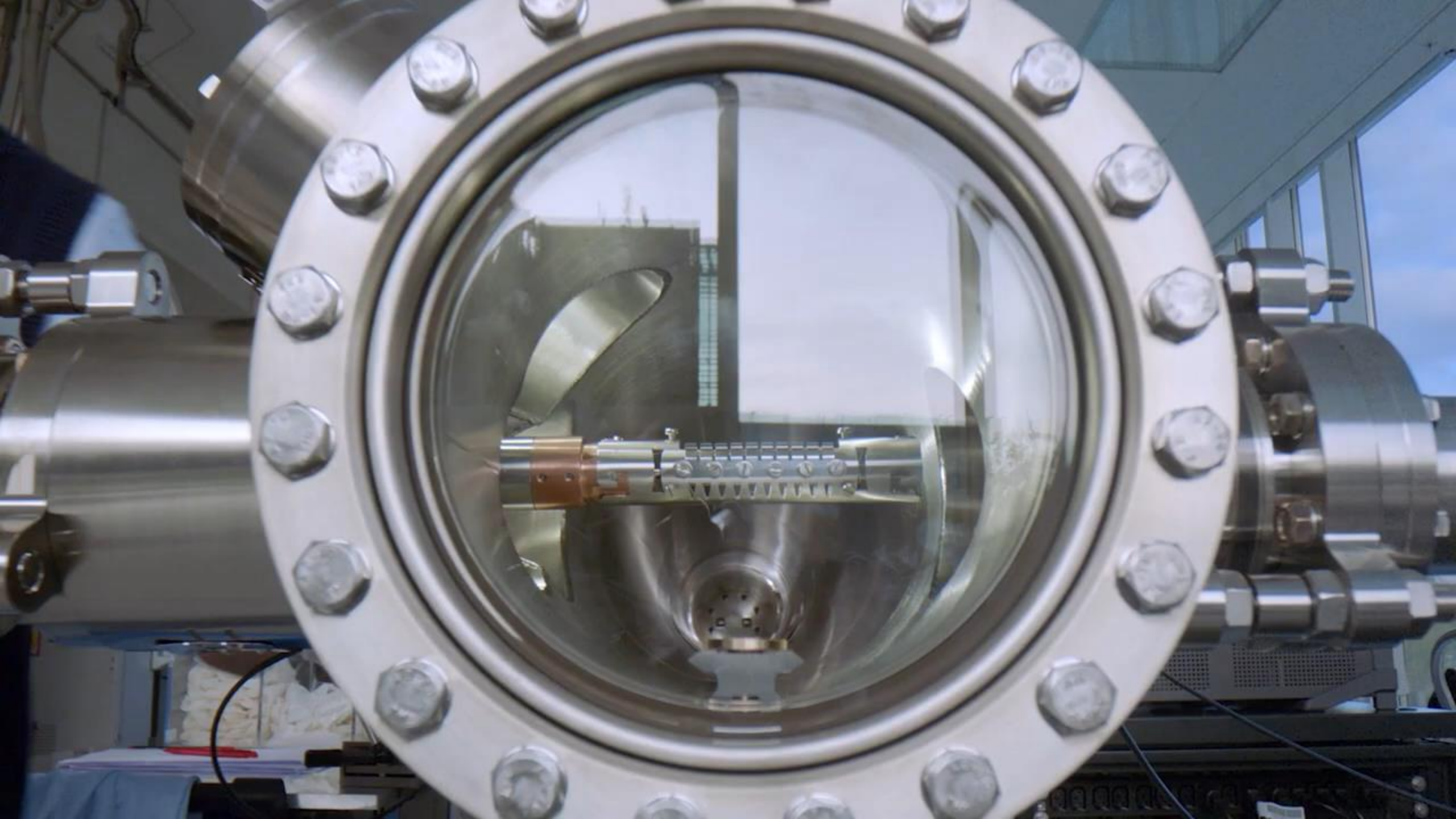
Dalla Torre, Reagor, *Simulating long-range coherence of atoms and photons in quantum computers*, *PRL* 2023



3) Optimal encoding of quantum states

Ben Dov, Shnaiderov, Makmal, Dalla Torre *Approximate encoding of quantum states using shallow circuits* arXiv:2207.00028





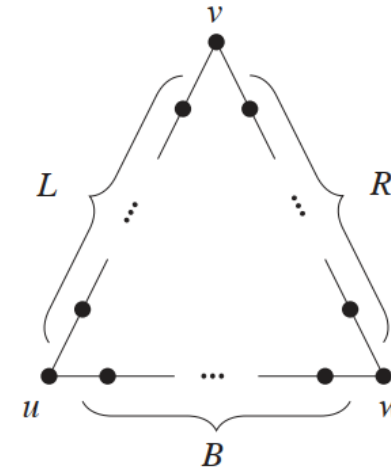
Non-local quantum games

a.k.a. Bell inequalities with many qubits

Example: “triangle game”

Bravyi, Gosset & König, Science 2018

Daniel & Myiaka, PRL 2021

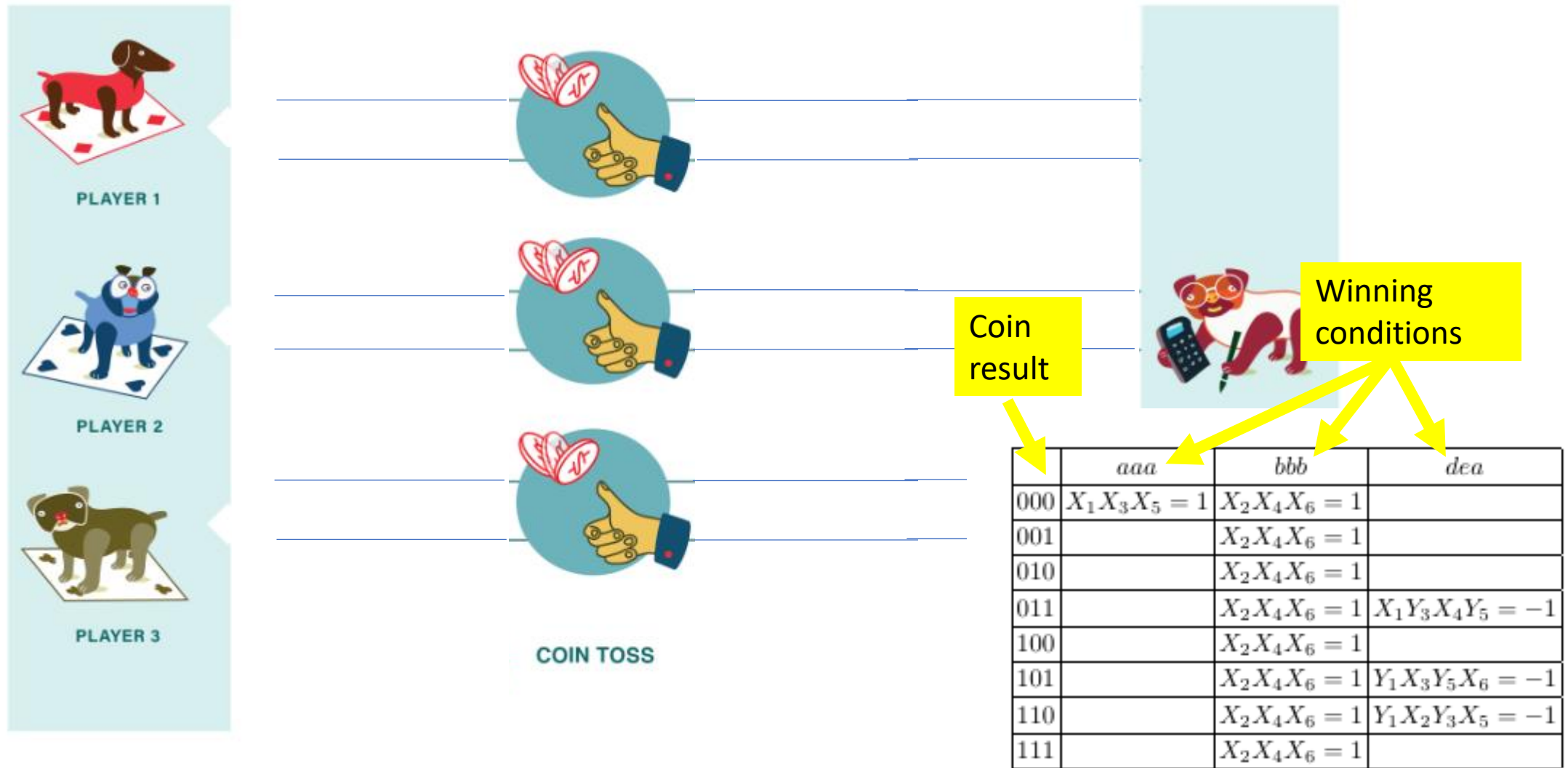


$$\langle P(\text{win}) \rangle_{\text{quantum}} = 1$$

$$\langle P(\text{win}) \rangle_{\text{classical}} < 7/8$$



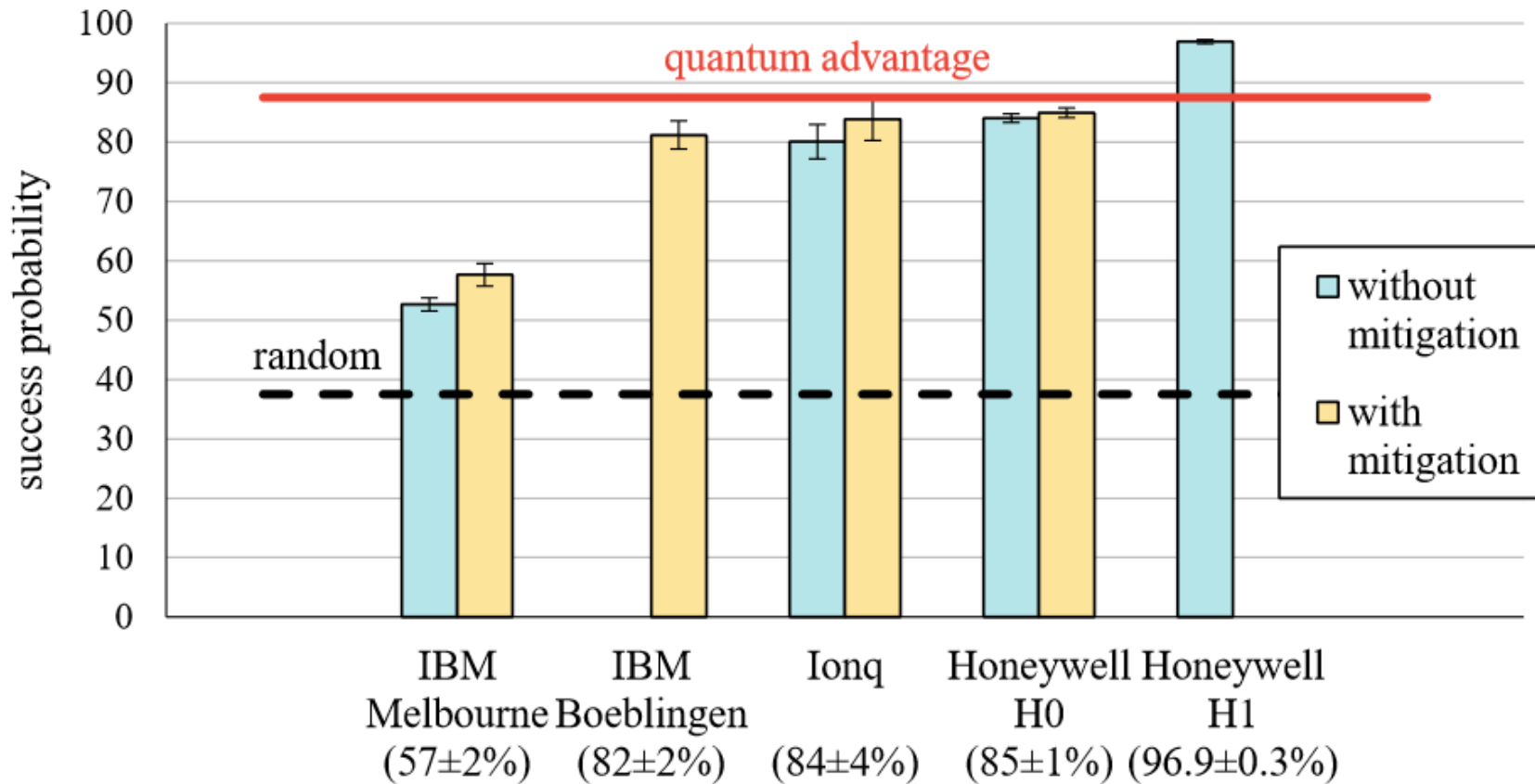
Minimal realization : 3 players = 6 qubits



$$\langle P(\text{win}) \rangle_{\text{classical}} < 7/8$$



Triangle game (6 qubit) : results



Sheffer, Azses, Dalla Torre, arXiv: 2105.05266
(See also: Daniel et al 2110.04277)



If all the students fail a test... lower the bar!

Stabilizers

$$s_i = Z_{i-1} X_i Z_{i+1}$$

$$s_i |\psi_{\text{cluster}}\rangle = |\psi_{\text{cluster}}\rangle$$

Sum of all products

$$S_{\text{all}} = 1 + \sum_i s_i + \sum_{i,j} s_i s_j + \dots$$

$$S_{\text{all}} |\psi_{\text{cluster}}\rangle = 2^n |\psi_{\text{cluster}}\rangle$$

	<i>aaa</i>	<i>bbb</i>	<i>dea</i>
000	$X_1 X_3 X_5 = 1$	$X_2 X_4 X_6 = 1$	
001		$X_2 X_4 X_6 = 1$	
010		$X_2 X_4 X_6 = 1$	
011		$X_2 X_4 X_6 = 1$	$X_1 Y_3 X_4 Y_5 = -1$
100		$X_2 X_4 X_6 = 1$	
101		$X_2 X_4 X_6 = 1$	$Y_1 X_3 Y_5 X_6 = -1$
110		$X_2 X_4 X_6 = 1$	$Y_1 X_2 Y_3 X_5 = -1$
111		$X_2 X_4 X_6 = 1$	

$$(S_{\text{all}})_{\text{classic}, n=6} \leq 28$$

Guhne, Toth, Hyllus, Briegel PRL (2005)

Optimal sum

$$S_{\text{optimal}} = \sum_{i,j} s_i s_j + \sum_{i,j,k} s_i s_j s_k + \sum_{i,j,k,l} s_i s_j s_k s_{k+1}$$

$$\langle S_{\text{optimal}} \rangle_{\text{IonQ}} = 41 \pm 0.5$$

$$(S_{\text{optimal}})_{\text{classic}, n=6} \leq 19$$

Cabello, Guhne, Rodriguez PRA (2008)

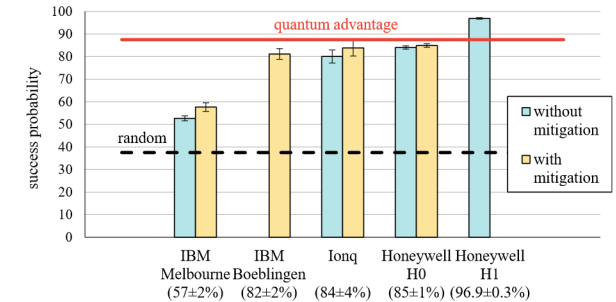


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What can you do with few qubits (and is it interesting?)

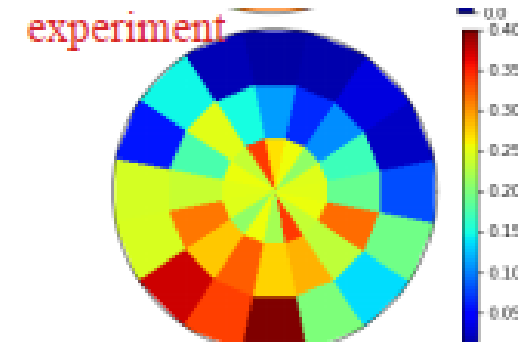
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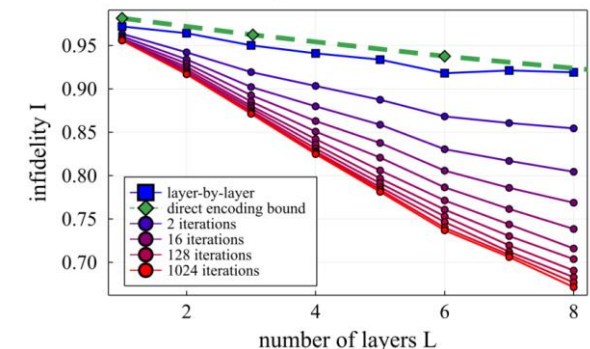
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Dalla Torre, Reagor, *Simulating long-range coherence of atoms and photons in quantum computers*, *PRL* 2023



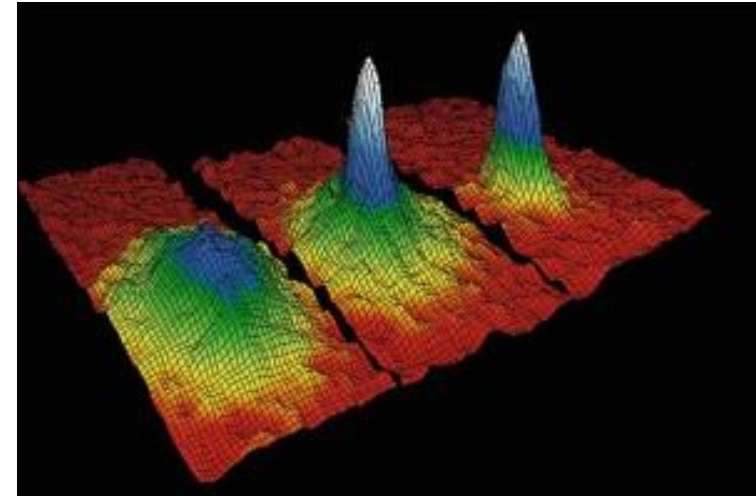
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Ben Dov, Shnaiderov, Makmal, Dalla Torre *Approximate encoding of quantum states using shallow circuits* arXiv:2207.00028



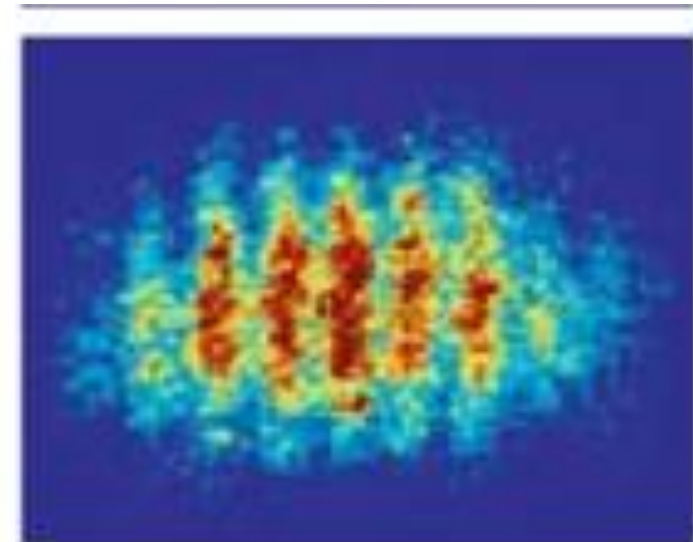
What is a Bose-Einstein condensate?

1. Macroscopic occupation of the ground state



Anderson et al, Science 1995

2. Interference / phase coherence



Schmiedmayer group 2005

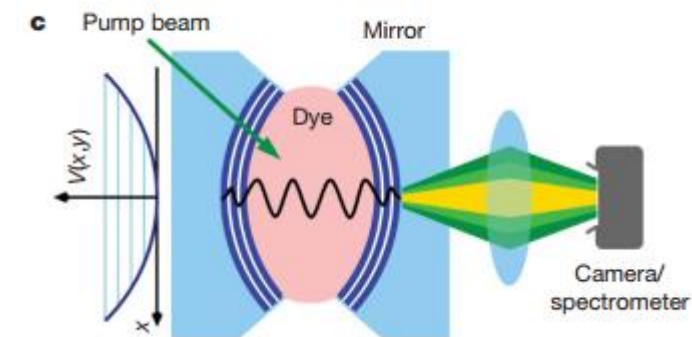
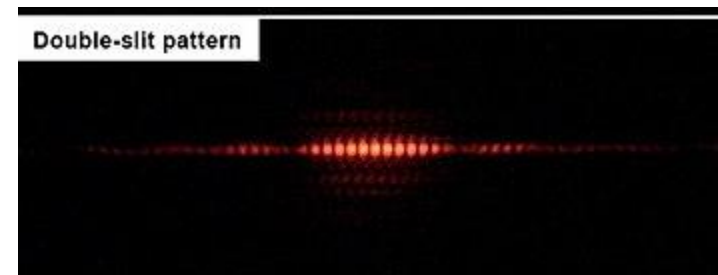
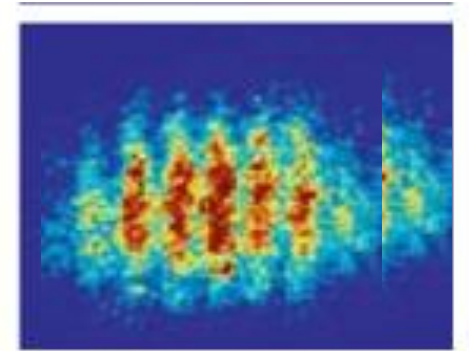


What is the difference between a BEC and a laser?

Our answer:
particle conservation!

$$[n, \phi] = i$$

- BEC: number of atoms conserved → no global phase
- laser: number of photons not conserved → global phase
- BEC of light (in dye molecules): photons number not conserved & no global phase



Our goal: simulate a BEC in a quantum computer

Step 1:

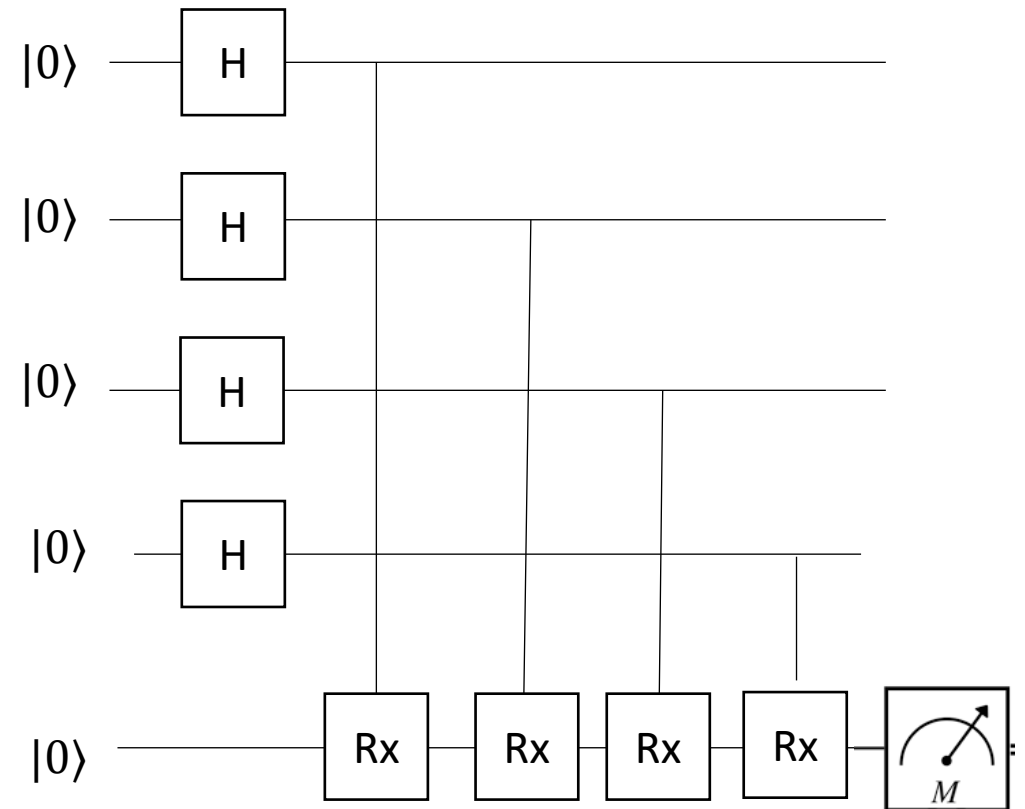
prepare a coherent state of qubit excitations
(analogous to the coherent state of a laser)

Step 2:

measure the total number of particles

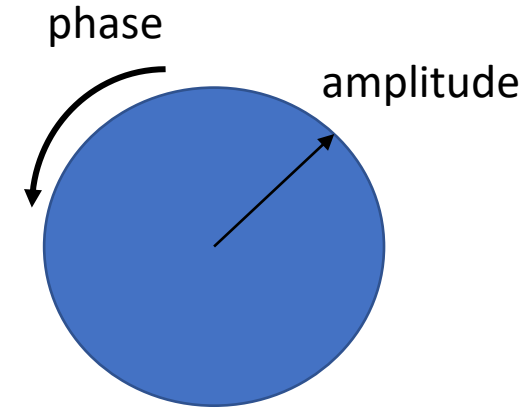
Step 3:

post-select the correct number

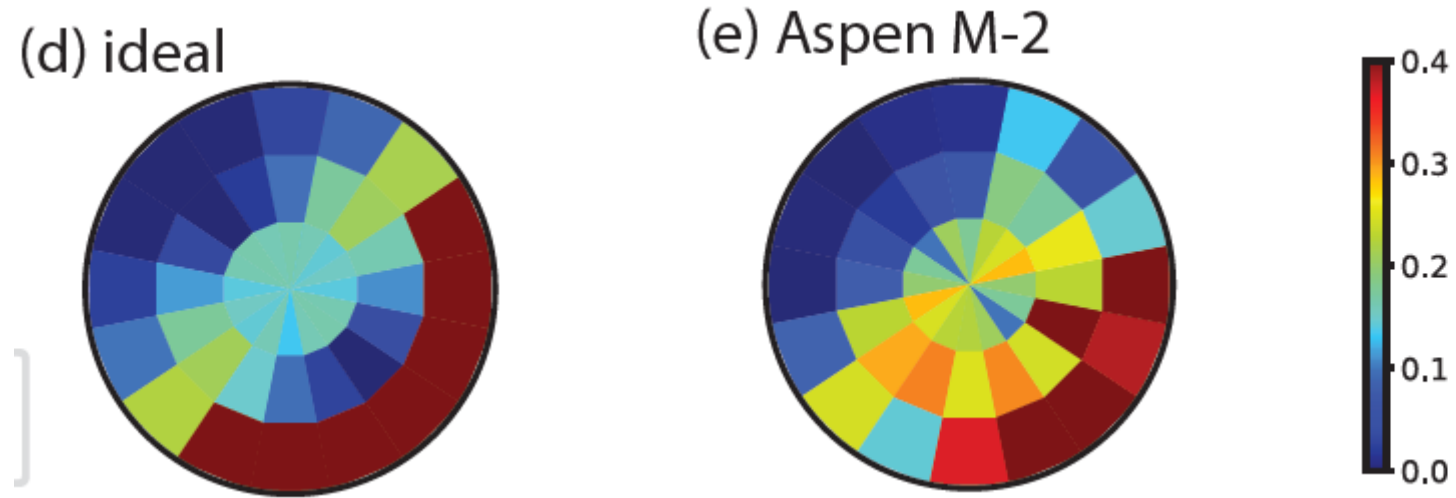


How to probe a BEC state?

Order parameter: $S_\theta = \cos(\theta)S_x + \sin(\theta)S_y$.



Results: 4 qubits + 1 ancilla



Why is this interesting?

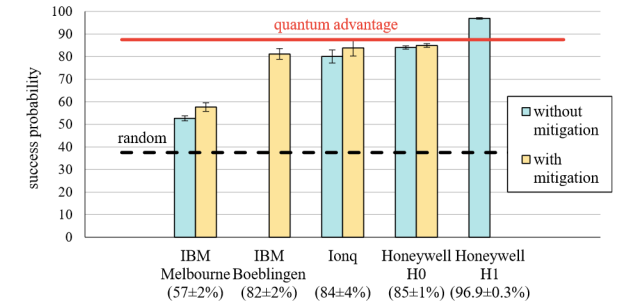
- Method to benchmark current quantum computers
- Quantum circuits: "new" theoretical framework
- The BEC state is more coherent than the laser state



What can you do with few qubits (and is it interesting?)

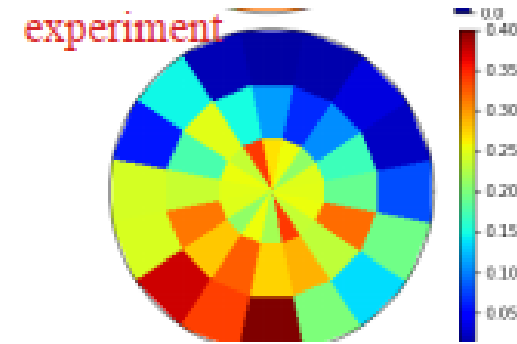
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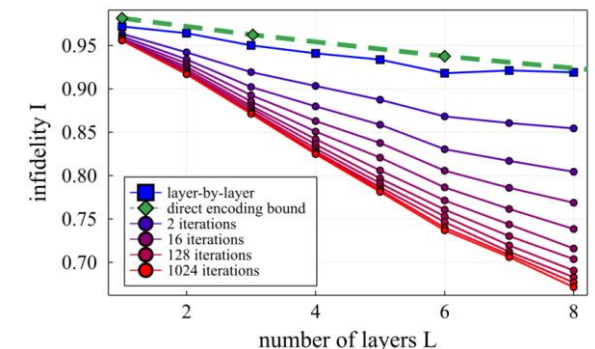
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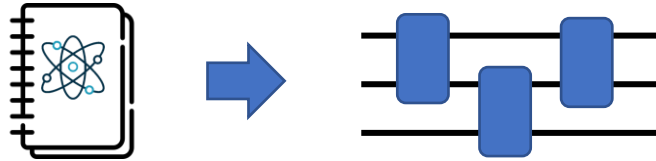
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Bar-Ilan University

Problem definition: quantum state encoding

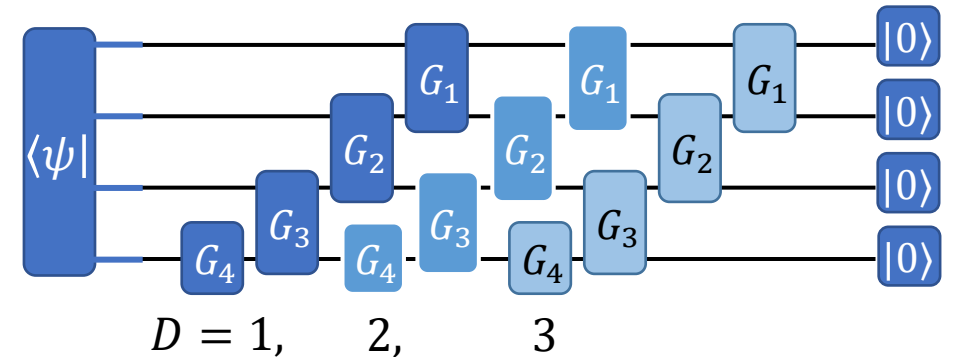


- Exact encoding of a quantum state **is hard**

$$N_{\text{gates}} \sim 2^{n_{\text{qubits}}}$$

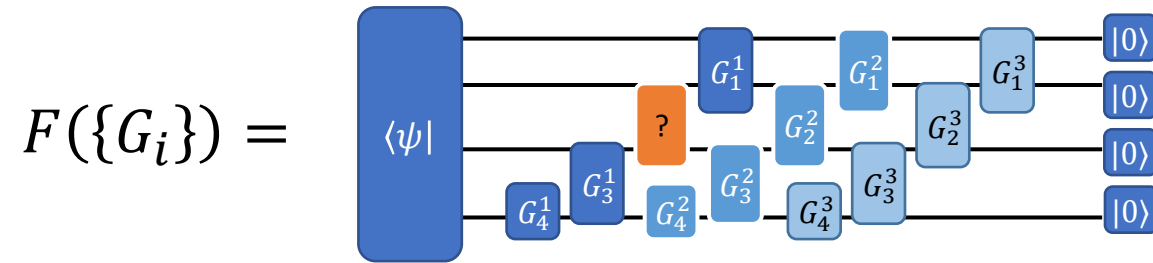
- Our approach: use approximate shallow encoder

$$N_{\text{gates}} \sim n_{\text{qubits}} \cdot D$$



Limited to target state with low-entanglement states (MPS)

Deterministic way to find the optimal encoding



1. Tensor tomography (16 Pauli strings)

$$\frac{dF}{dG_{2\alpha,\beta}^1 \gamma,\delta} = \langle \tilde{\psi}_1 | \begin{array}{c} \alpha \quad \gamma \\ \beta \quad \delta \end{array} | \tilde{\psi}_2 \rangle = \begin{array}{c} \alpha \\ \beta \end{array} \begin{array}{c} \frac{dF}{dG} \end{array} \begin{array}{c} \gamma \\ \delta \end{array}$$

2. Find with the best unitary gate

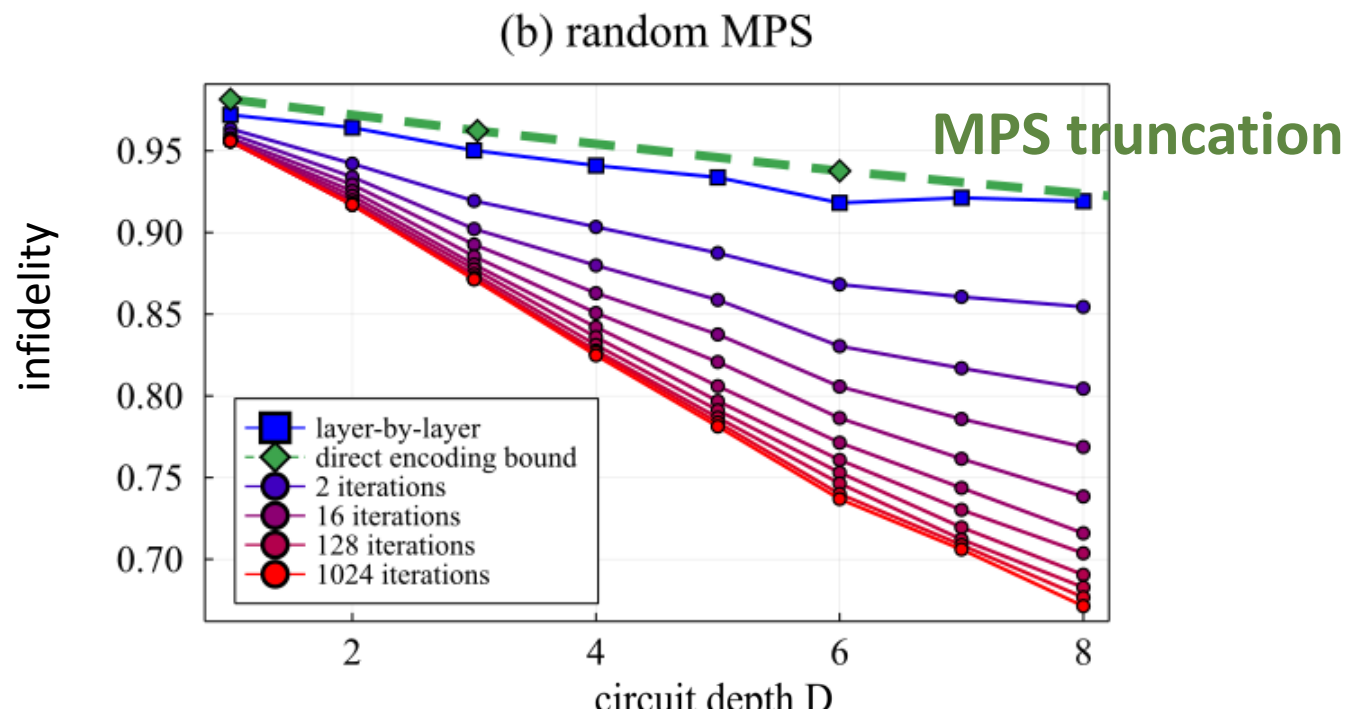
$$G_{new} = \left(\frac{dF^\dagger}{dG} \right)_{\text{unitary}}$$

$$A = U S V^\dagger \Rightarrow (A)_{\text{unitary}} = U V^\dagger$$

3. Repeat for each gate and loop

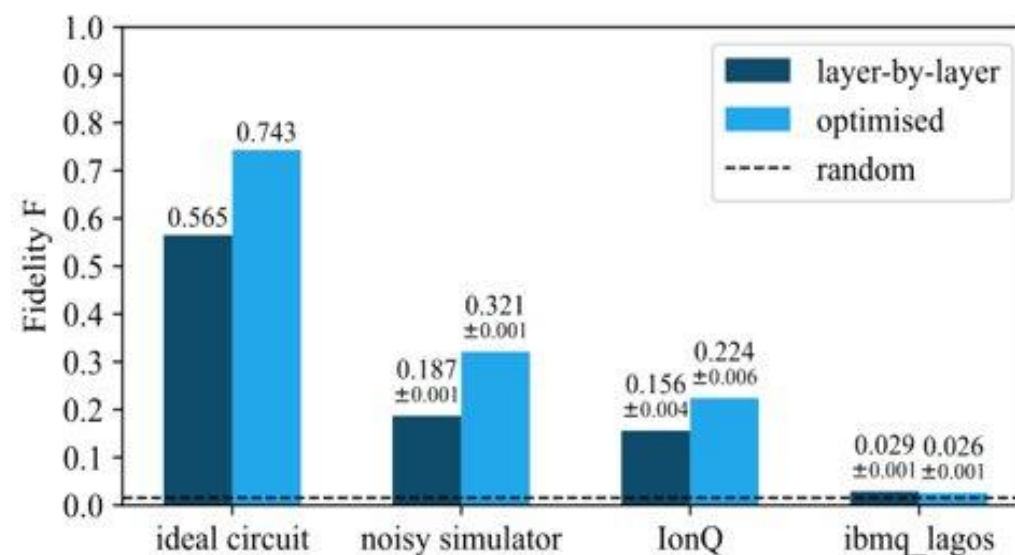
Results

1. Optimal encoding of random MPS
(20 qubits)

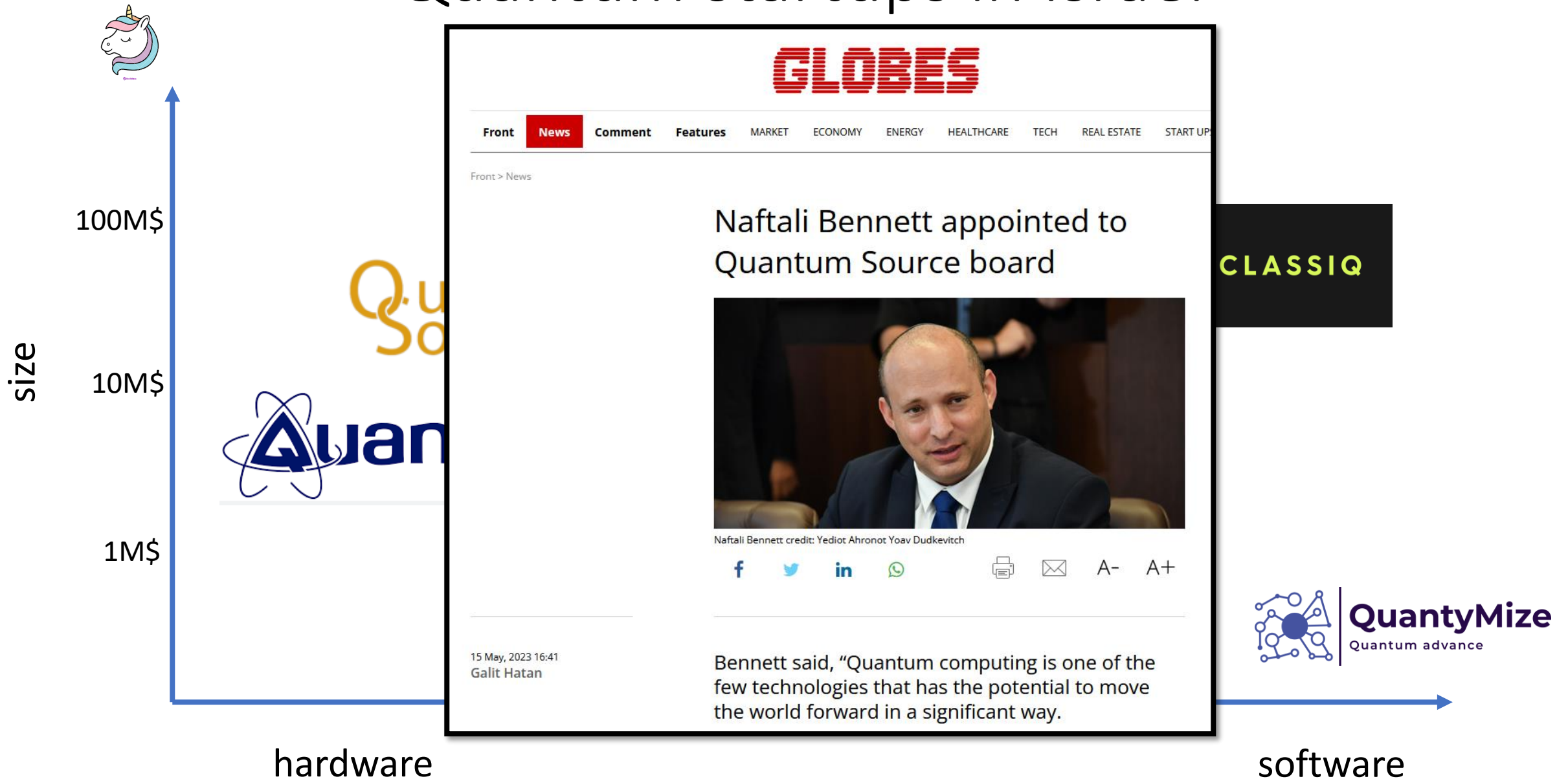


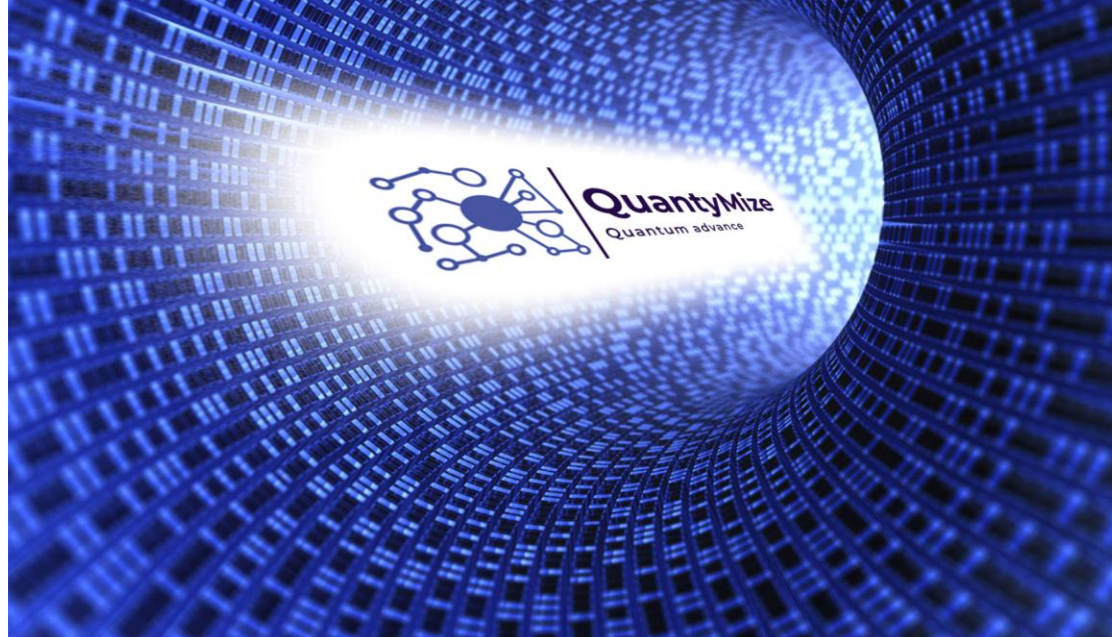
2. Experiment with 6 qubits

3. Shot noise -> Barren plateaux
Solution: use local cost function

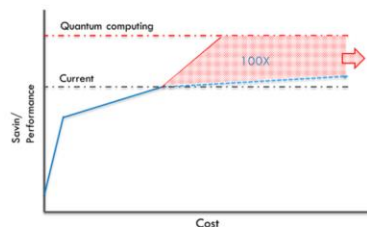
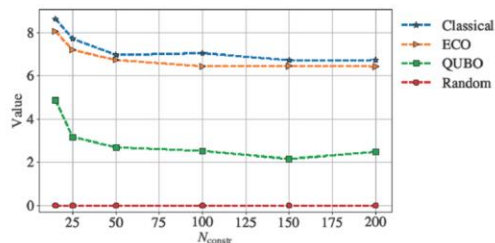


Quantum startups in Israel



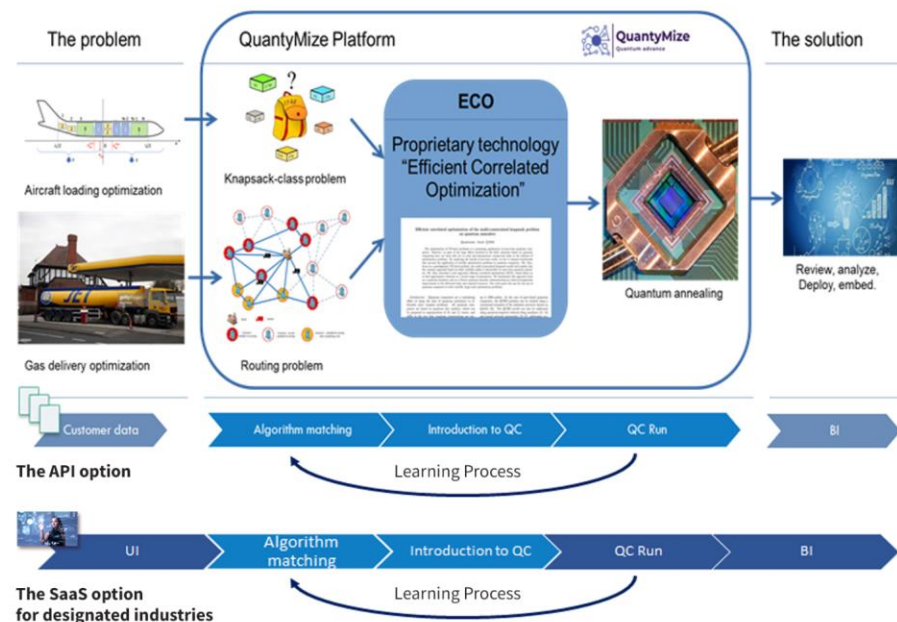


- **Quanty Mize - Founded in 2022**
- Team: 7 experts (industry, academy, 2 PhD , AI and technology experts)
- **Purpose: Enabling 100x optimization capabilities using quantum computing**
Solving large scale industry NP hard problems;
Infrastructure middleware based on proprietary algorithms and machine learning breakthrough in optimization
- ECO[®] (Efficient Correlated Optimization) Quantum advance algorithm developed paves the way for the use of quantum computers to solve real-life, large-scale optimization problems. delivers a **100X improvement** in the size of the problem that can be solved efficiently using quantum computers
- **Currently at seed funding stage: Raising \$3M**



How we are solving that

- Platform with runtime segment oriented
- Infrastructure middleware based on proprietary algorithms and Machine Learning: breakthrough in optimization
- Interface to most advanced and scalable quantum computing infrastructure
- Current focus: combinatorial optimization for foodtech, finance, resource allocation, logistics and more



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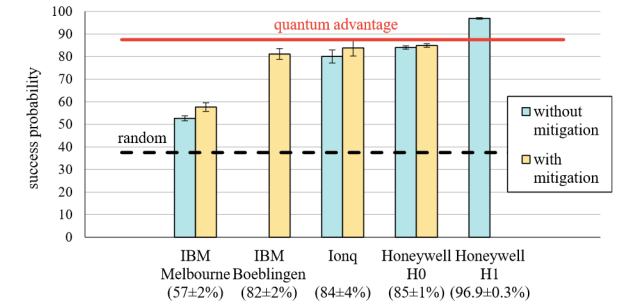
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Quantum Simulations using quantum computers on the cloud

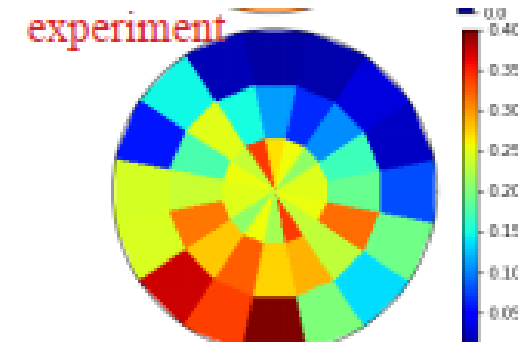
1) Non local games with 6 qubits

Sheffer, Azses, Dalla Torre, *Playing nonlocal games with 6 noisy qubits on the cloud*, *Adv. Quant. Tech* 2021



2) Simulating a BEC with 5 qubits

Dalla Torre, Reagor, *Simulating long-range coherence of atoms and photons in quantum computers*, *PRL* in press



3) Optimal encoding of quantum states

Ben Dov, Shnaiderov, Makmal, Dalla Torre *Approximate encoding of quantum states using shallow circuits* arXiv:2207.00028

