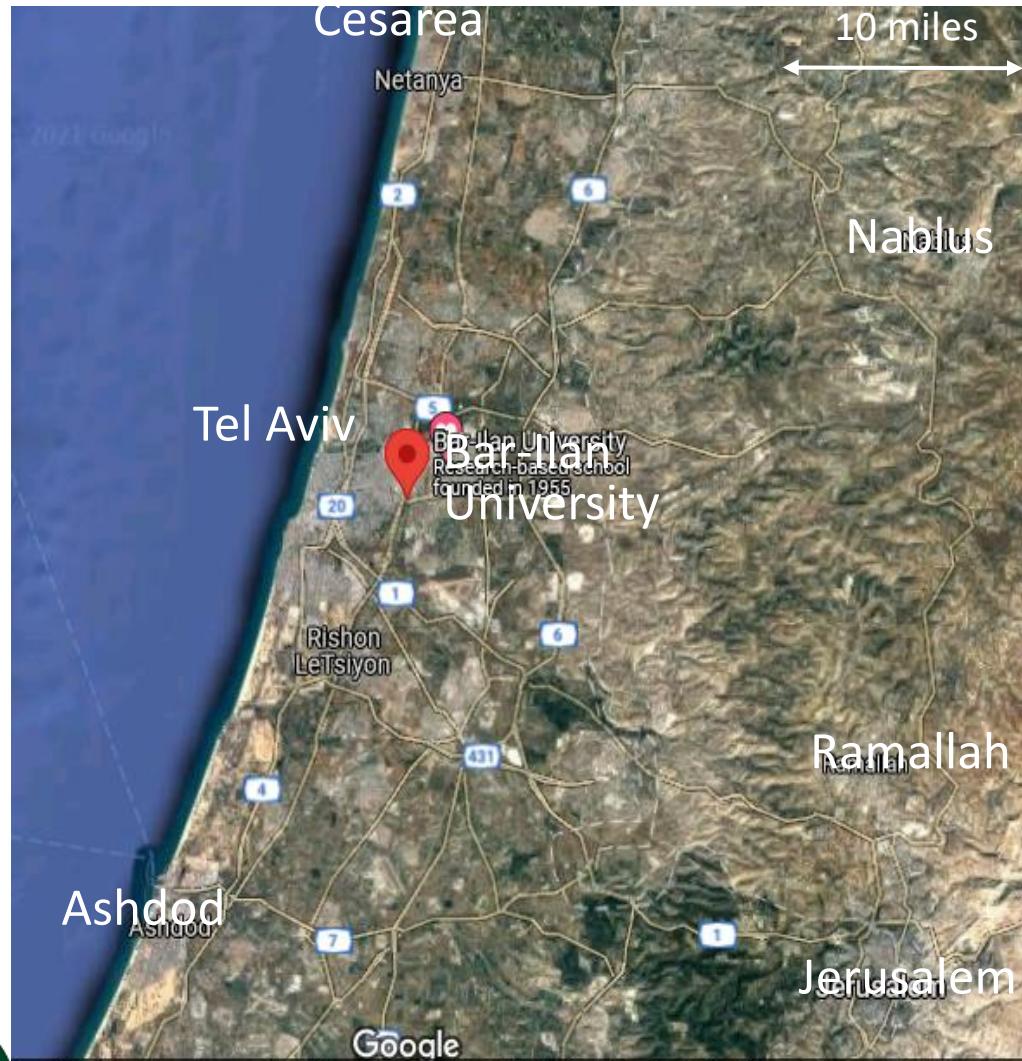


Parametric oscillators: Ising machines, prethermalization, and squeezing

Emanuele Dalla Torre

Bar-Ilan University

Bar-Ilan University (established 1955)



Bar-Ilan University



Emanuele Dalla Torre

Dynamics of complex quantum systems



David Dentelski
(→Q. Source)



Inbar Shani
(→Weizmann)



Marcello Calvanese
Strinati (→CNR Rome)



Atanu Rajak
(→Presidency U
Kolkata → IITH)



Yonathan Saadia
(→IDF)



Leon Bello
(→Princeton)



Michael Stern
Bar-Ilan University



Avi Pe'er



Itzhack Dana



Roberta Citro
(Salerno)



Takashi Oka
(Tokyo)



rigetti

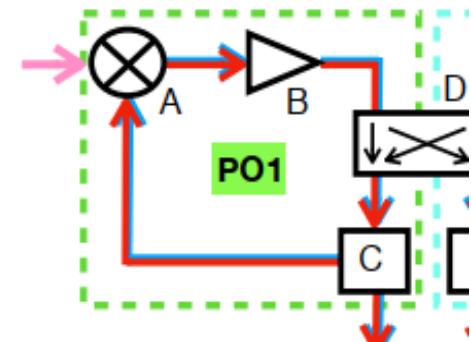
Microsoft

Parametric drives are cool!

Classical → coherent Ising machines

L. Bello, M. Calvanese Strinati, EGDT, A. Pe'er, PRL&PRA 2020, NJP 2020

M. Calvanese Strinati, L. Bello, EGDT, A. Pe'er, PRL 2021



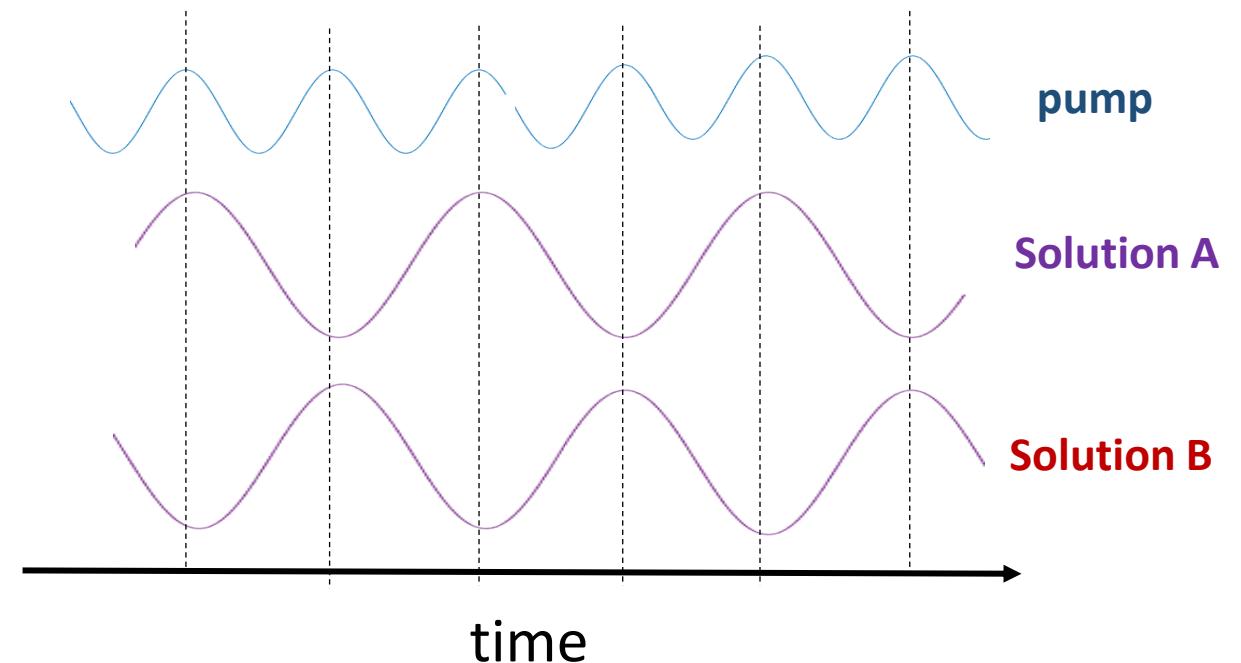
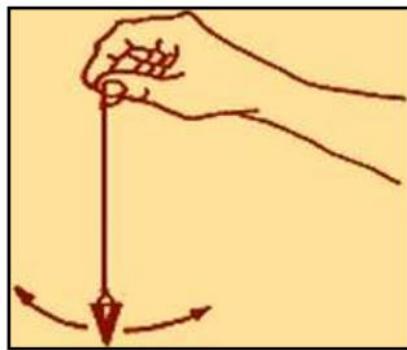
Many-body → Floquet prethermalization

Quantum → anti-squeezing



Classical parametric resonance

$$F(t) = (-g + \delta \cos(2\Omega t)) \sin \theta$$



Stability: Mathieu equation (1868)

$$\ddot{\theta}(t) = (-g + \delta \cos(2\Omega t))\theta(t)$$

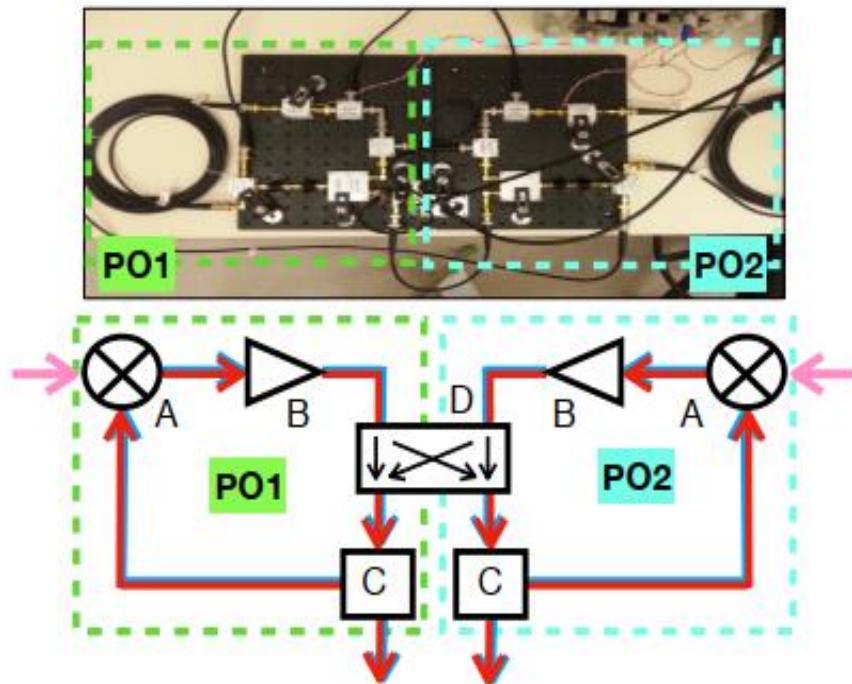
Period doubling, a.k.a. discrete time crystal

Two solutions = 1 bit

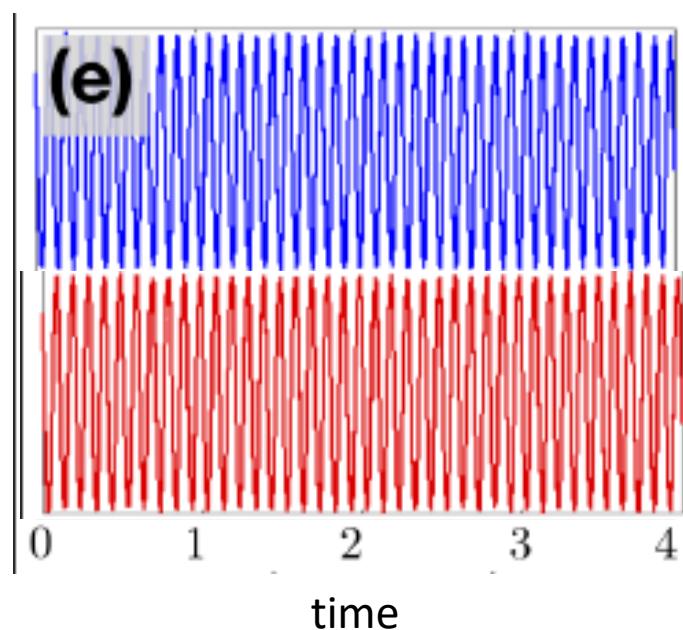


Two coupled parametric oscillators

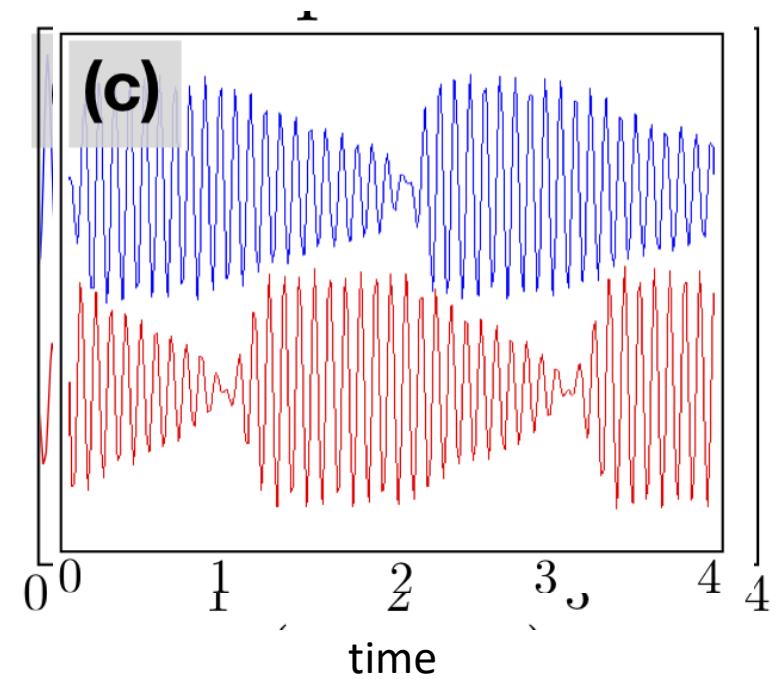
Coaxial cables: microwave oscillators



Naïve expectation



Experiment: beating!

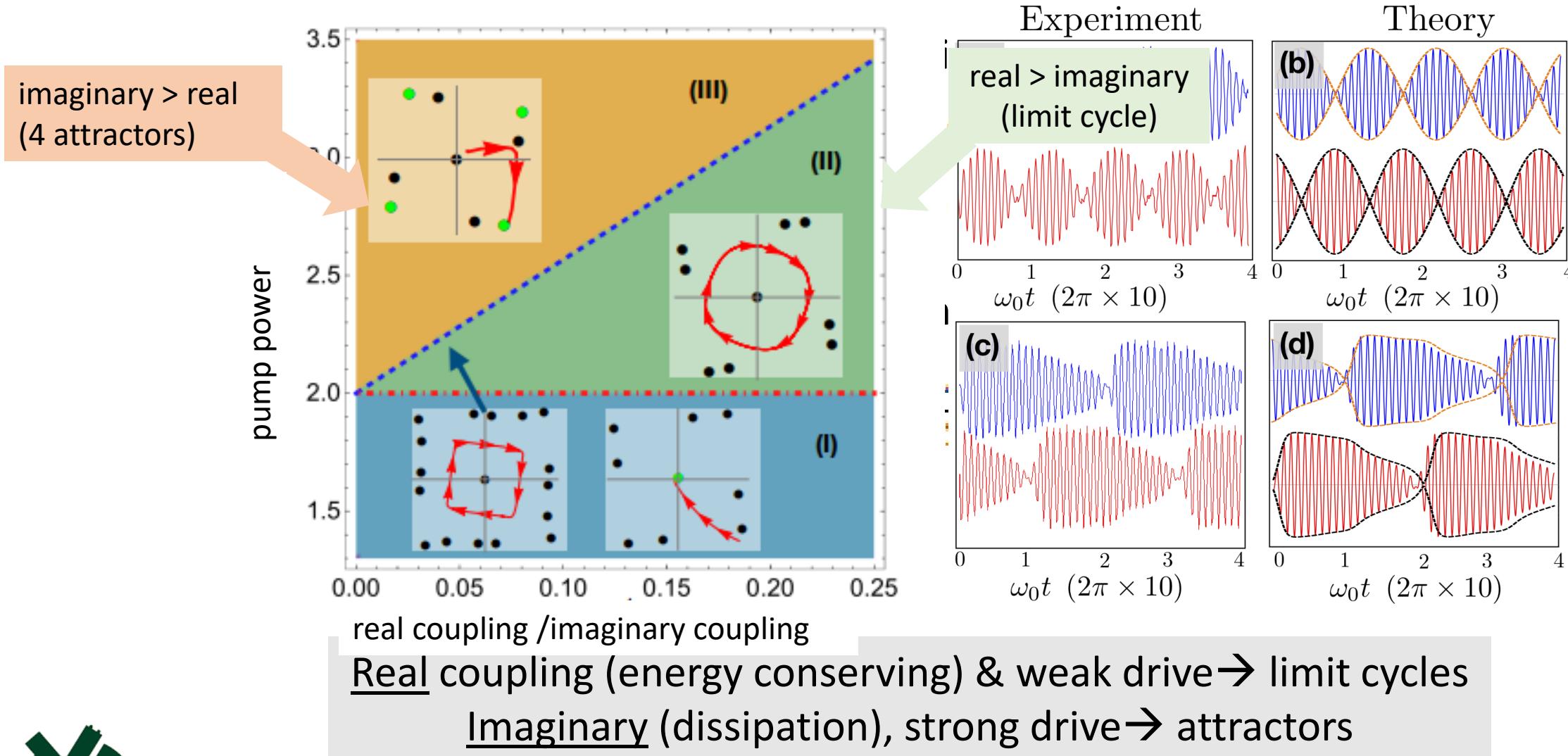


L. Bello, M. Calvanese Strinati, E. G. Dalla Torre, A. Pe'er, PRL&PRA (2020), NJP (2020)

Bar-Ilan University

Emanuele Dalla Torre

Two coupled parametric oscillators - theory



Many coupled PO - Coherent Ising machines (CIM)

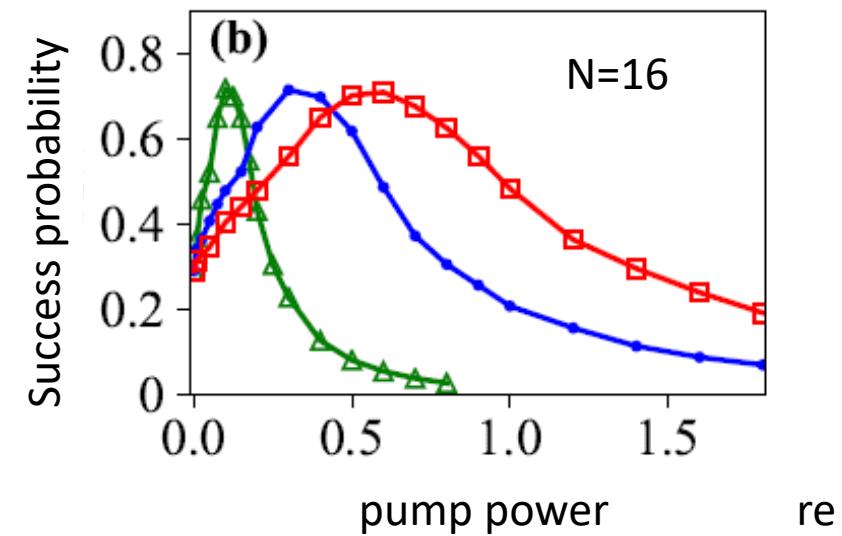
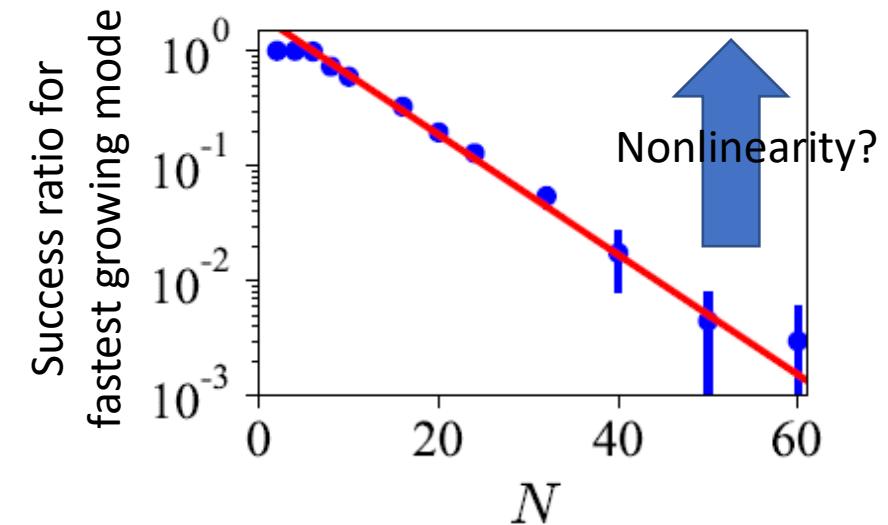
Coupling encoded in the dissipative term: $\frac{dE}{dt} = \sum_{i,j} J_{i,j} \sigma_i \sigma_j$

Review: Yamamoto et al, npj quant. info. (2017)

- Linear approximation: mode competition
(BUT finding the maximal eigenvalue of $J_{i,j}$ not NP hard!)

- Nonlinearities can help find the correct solution (heuristics)

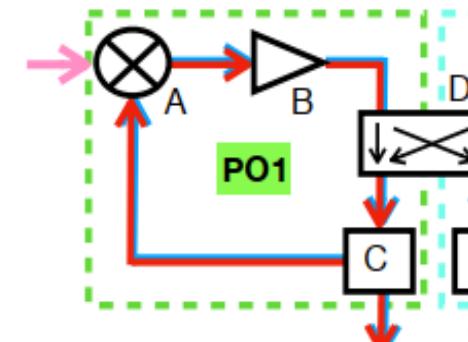
M. Calvanese Strinati, L. Bello, EGDT, A. Pe'er, PRL (2021)



Parametric drives are cool!

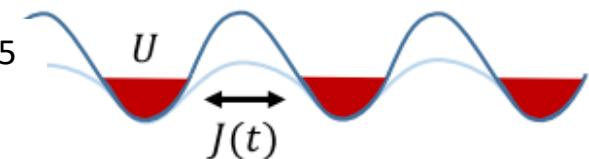
Classical → coherent Ising machines

L. Bello, M. Calvanese Strinati, EGDT, A. Pe'er, PRL&PRA 2020, NJP 2020
M. Calvanese Strinati, L. Bello, EGDT, A. Pe'er, PRL 2021



Many-body → Floquet prethermalization

Coupled Oscillators:	Citro, Dalla Torre et al, Ann. of Phys., 2015 Rajak, Citro, Dalla Torre, JPA, 2018 Rajak, Dana, Dalla Torre, PRB (R), 2019 Saadia, EGDT, Rajak, PRR, 2019
Bose-Hubbard model:	EGDT, Dentelski, Scipost 2021
Review:	Wen Wei Ho, Takashi Mori, Dmitry Abanin, EGDT, Ann Phys 2023



Quantum → anti-squeezing



Periodically driven optical lattices

$$H = \sum_i U n_i^2 + J(t) (b_i^\dagger b_j + H.c.)$$

$$J(t) = J_0 + \delta J \cos(\Omega t)$$

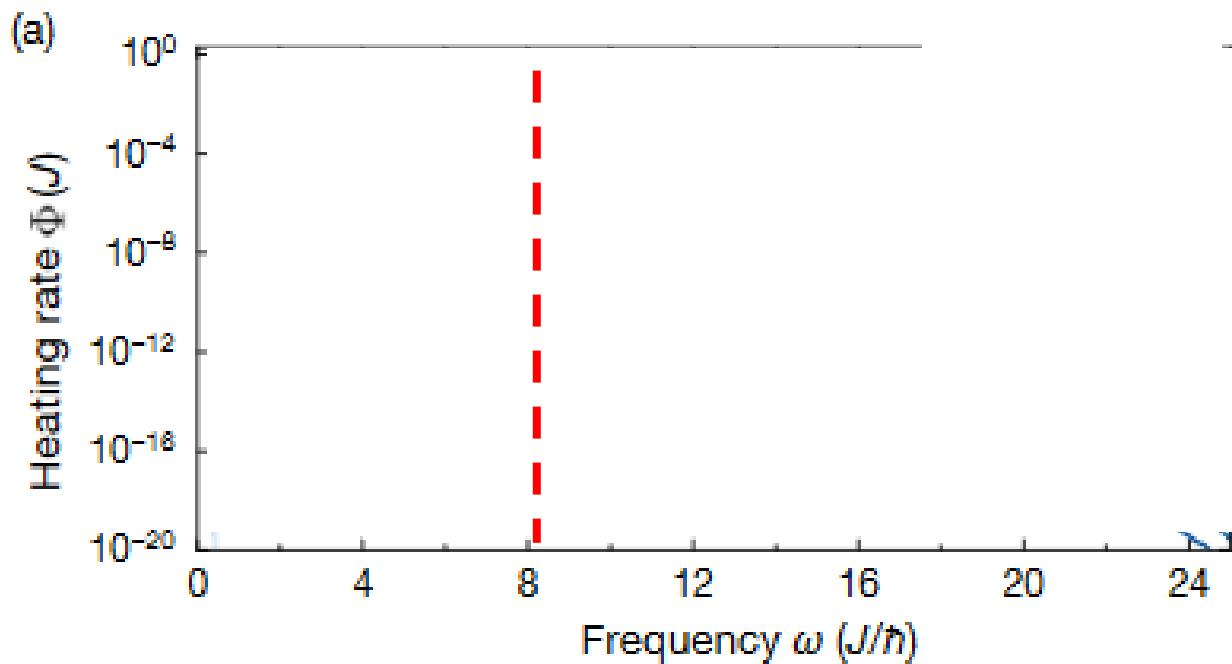
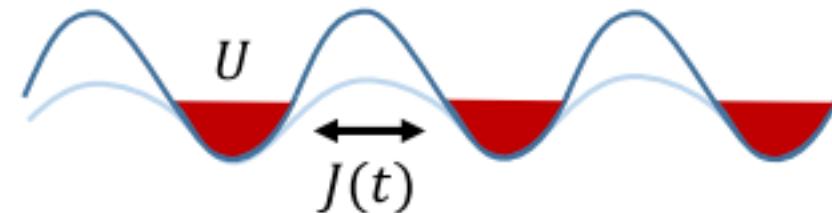
Number and phase

$$H(t) = \sum_i \frac{U}{2} n_i^2 - J(t) \cos(\phi_i - \phi_j)$$

Quadratic approximation:

$$H(t) = \sum_q \frac{U}{2} n_q^2 + 2J(t) \sin(q) \phi_q^2$$

Atanu Rajak, Roberta Citro, EGDT, JPA (2018)



Rubio Abadal et al (I. Bloch group), PRX 2022

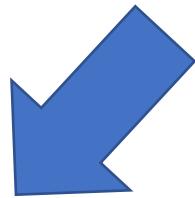
Emanuele Dalla Torre



Bar-Ilan University

Floquet prethermalization

$$\frac{dE}{dt} \sim e^{-\Omega/\Lambda}$$



Rigorous theorems for quantum spin chains

bounded local Hamiltonian

$$\frac{dE}{dt} \sim \epsilon \frac{\Omega}{\Lambda} \sim \exp\left(-\frac{\Omega}{\Lambda}\right)$$

Abanin, De Roeck, Ho, Huveneers (PRL 2015, CMP 2017) -
Kuwahara, Mori, Saito, (Ann.of.Phys 2015, PRL 2015)

Statistical argument for classical systems

Rajak, Citro, Dalla Torre, JPA (2018)
Rajak, Dana, Dalla Torre, PRB (R) (2019)



Statistical Floquet prethermalization

- Boltzmann distribution → Exponentially low probability of finding a many-body resonance

- Application to the Bose-Hubbard model:

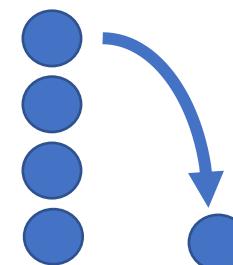
EGDT, Dentelski, Scipost 2021

- Transient behavior (coupled rotors)

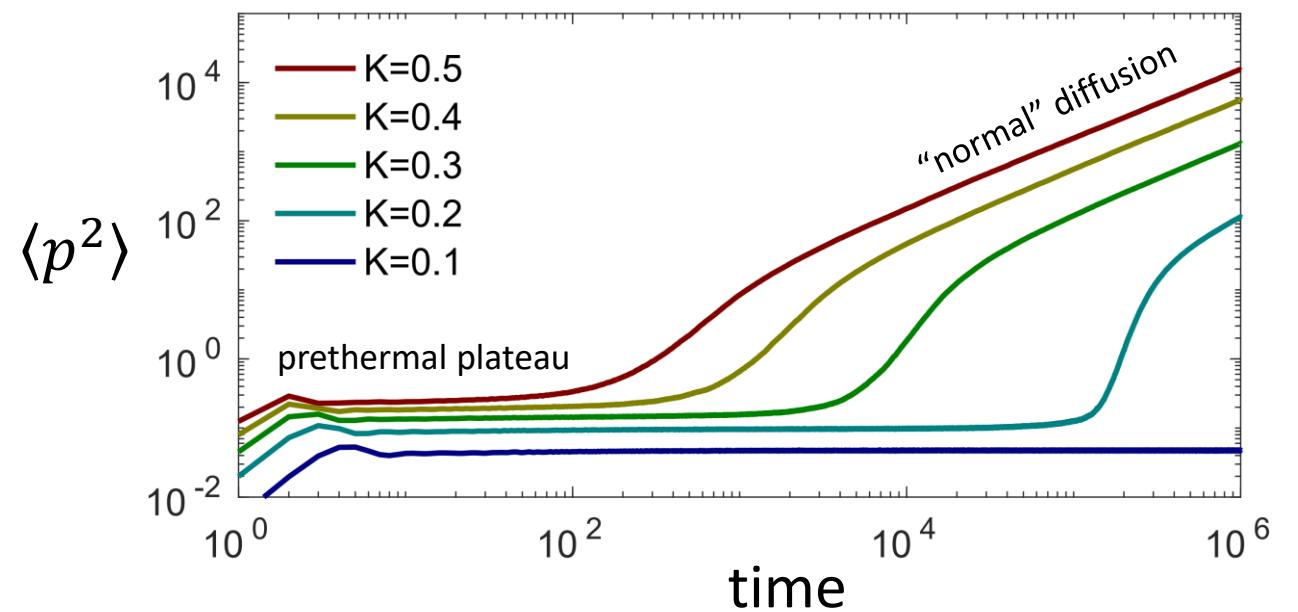
A. Rajak, R. Citro, EGDT, JPA (2018)

A. Rajak, Dana, Dalla Torre, PRB (R) (2019)

Prethermal timescale $\tau \sim e^{\Omega/\Lambda}$



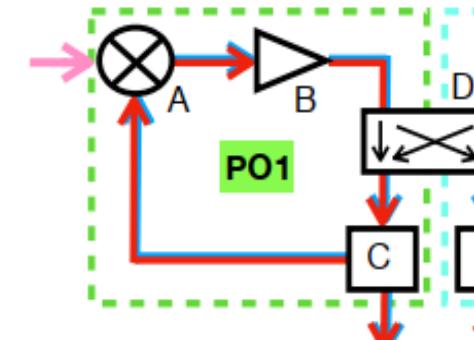
$$E = \frac{U}{2} n(n - 1) \Rightarrow \Delta E = U \Delta n$$



Parametric drives are cool!

Classical → coherent Ising machines

L. Bello, M. Calvanese Strinati, EGDT, A. Pe'er, PRL&PRA 2020, NJP 2020
M. Calvanese Strinati, L. Bello, EGDT, A. Pe'er, PRL 2021



Many-body → Floquet prethermalization

Coupled Oscillators: Citro, Dalla Torre et al, Ann. of Phys., 2015

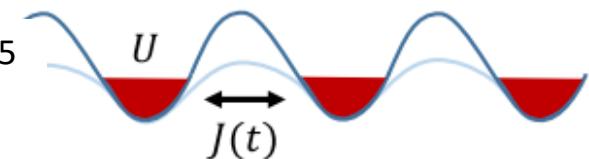
Rajak, Citro, Dalla Torre, JPA, 2018

Rajak, Dana, Dalla Torre, PRB (R), 2019

Saadie, EGDT, Rajak, PRR, 2019

Bose-Hubbard model: EGDT, Dentelski, Scipost 2021

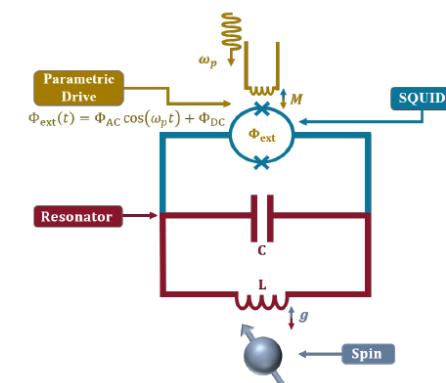
Review: Wen Wei Ho, Takashi Mori, Dmitry Abanin, EGDT, Ann Phys 2023



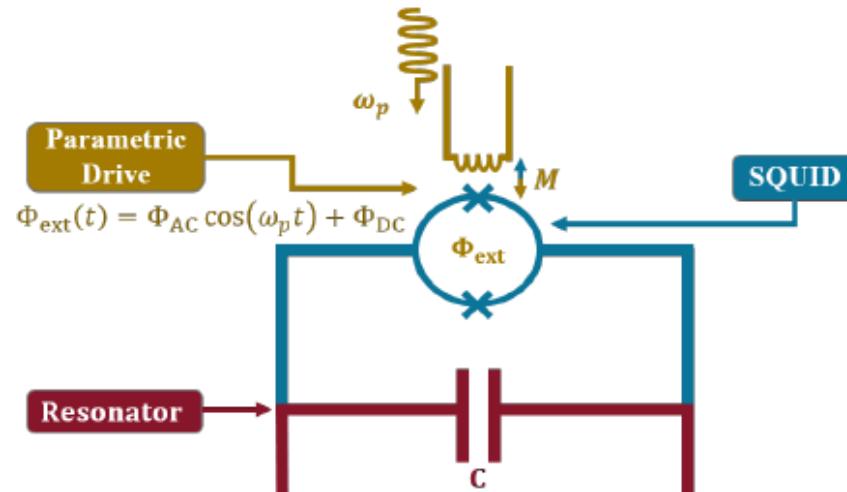
Quantum → anti-squeezing

Theory: Inbar Shani, EGDT, Michael Stern, PRR 2021

Experiment: Villiers et al (Kondos&Leghtas group), arxiv 2023

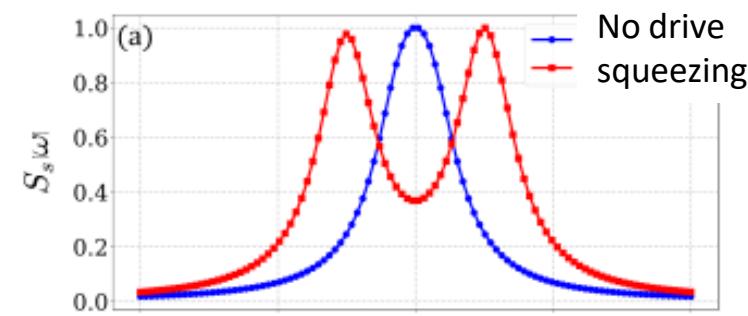


Parametrically pumped resonator (squeezing)



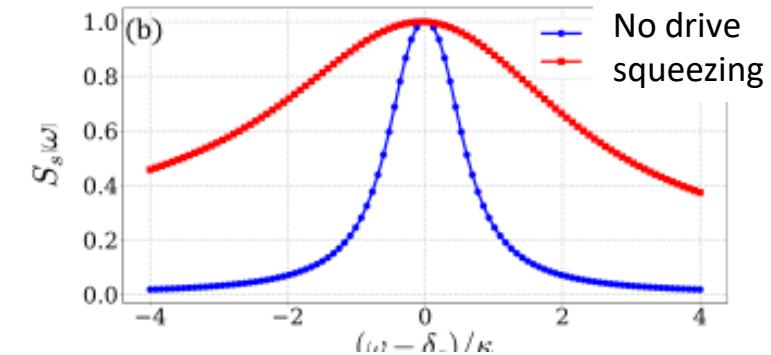
$$\tilde{H}/\hbar = \Omega_r \gamma^\dagger \gamma + \frac{1}{2} \tilde{\omega}_s \sigma_z + \frac{1}{2} g e^r (\gamma^\dagger + \gamma)(\sigma_+ + \sigma_-) - \frac{1}{2} g e^{-r} (\gamma^\dagger - \gamma)(\sigma_+ - \sigma_-).$$

$$\begin{cases} \gamma = a \cosh(r) - a^\dagger \sinh(r) \\ \gamma^\dagger = a^\dagger \cosh(r) - a \sinh(r) \end{cases}$$



Leroux, Govia, Clerk PRL, 2018

$L = \text{squeezed vacuum}$



Shani, Dalla Torre, Stern, PRR 2022

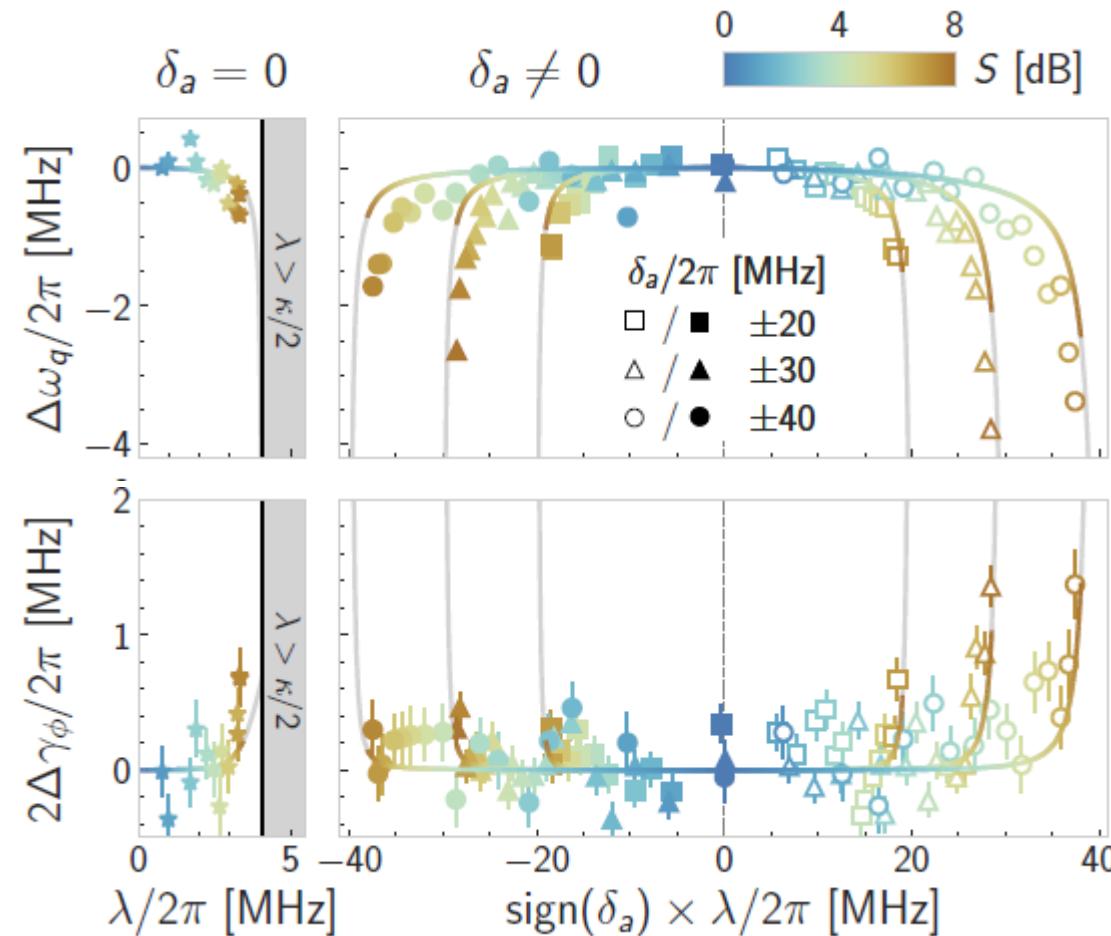
$L = \text{normal vacuum}$



$$\frac{d}{dt} \rho = -\frac{i}{\hbar} [\tilde{H}, \rho] + L \rho L^\dagger - \frac{1}{2} (L^\dagger L \rho + \rho L^\dagger L)$$

Squeezing: two competing effects

Enhanced dispersive shift:



Enhanced dephasing:

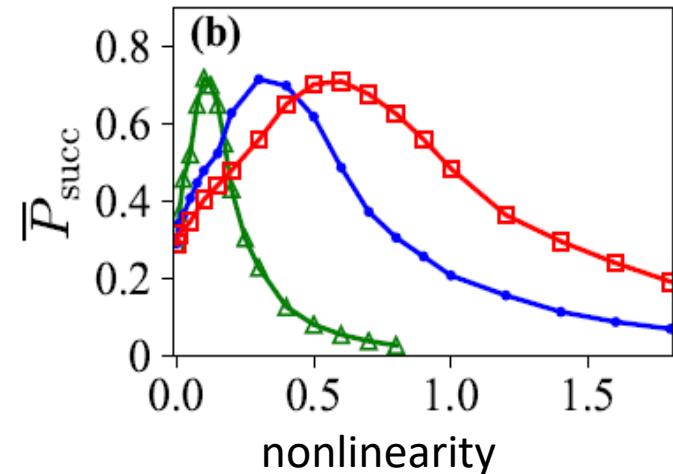
Theory: Inbar Shani, EGDT, Michael Stern, PRR 2021
Experiment: Villiers et al (Kondos&Leghtas group), arxiv



Summary: what did we learn?

Classical → energy-preserving coupling = limit cycles

L. Bello, M. Calvanese Strinati, EGDT, A. Pe'er, PRL&PRA (2020), NJP (2020)
M. Calvanese Strinati, L. Bello, EGDT, A. Pe'er, PRL (2021)

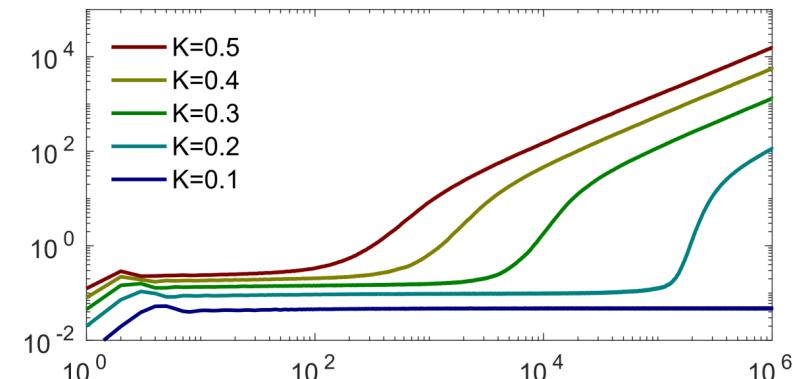


Many-body → statistical Floquet prethermalization $\frac{dE}{dt} \sim e^{-\frac{\Omega}{\Lambda}}$

Coupled Oscillators: Citro, Dalla Torre et al, Ann. of Phys., 2015
Rajak, Citro, Dalla Torre, JPA, 2018
Rajak, Dana, Dalla Torre, PRB (R), 2019
Saadia, EGDT, Rajak, PRR, 2019

Bose-Hubbard model: EGDT, Dentelski, Scipost 2021

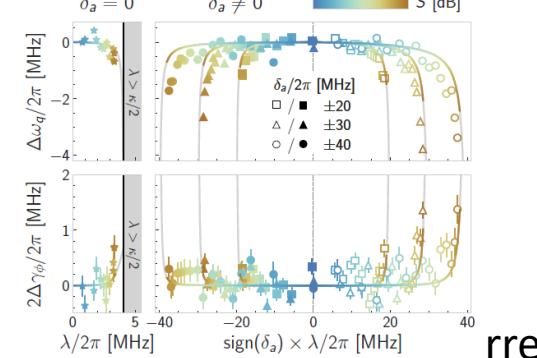
Review: Wen Wei Ho, Takashi Mori, Dmitry Abanin, EGDT, arxiv 2022



Quantum → squeezing enhances coupling and dephasing

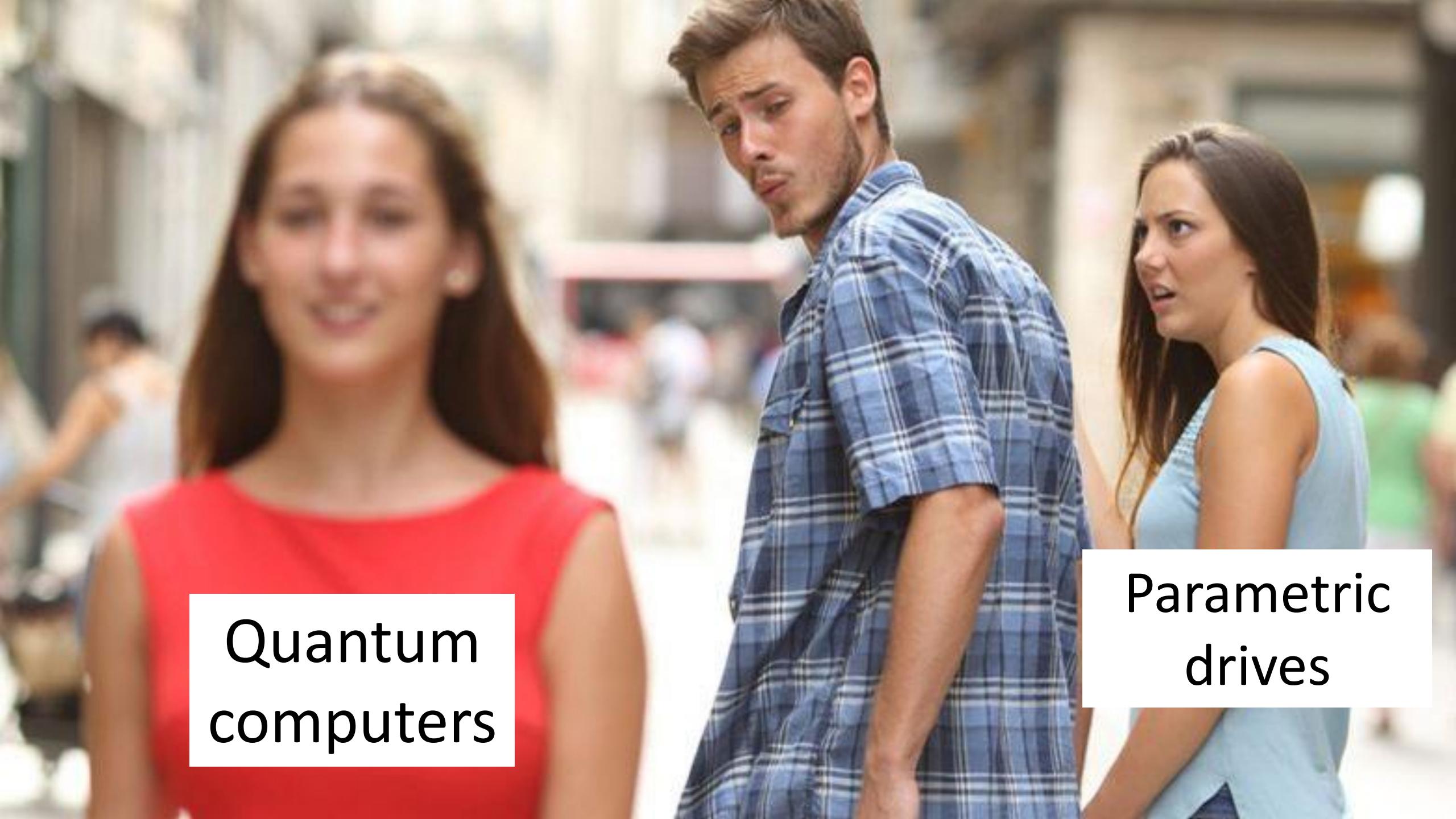
Theory: Inbar Shani, EGDT, Michael Stern, PRR 2021

Experiment: Villiers et al (Kondos&Leghtas group), arxiv



Bonus Slides



A photograph of a man in a blue and white plaid shirt looking back over his shoulder at two women. A woman in a red top is on the left, and a woman in a light blue top is on the right. The man has a surprised or confused expression.

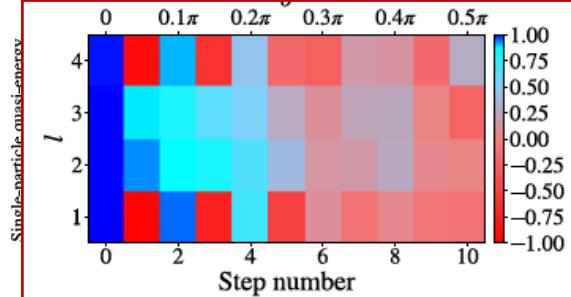
Quantum
computers

Parametric
drives

Quantum simulations on quantum computers

Actual results on real hardware with up to 6 qubits

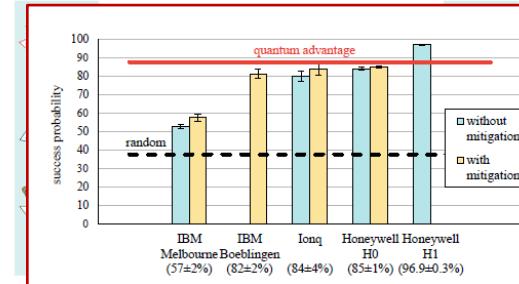
Topological phases in 1d



PRL 2020, PRB 2021



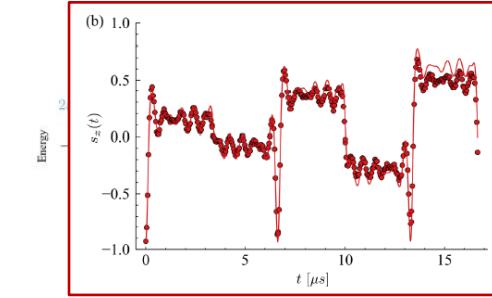
Nonlocal games



Adv Q Tech 2022



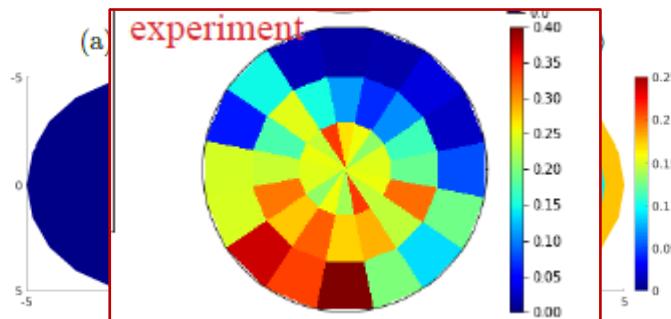
Long-range interactions



PRR 2021

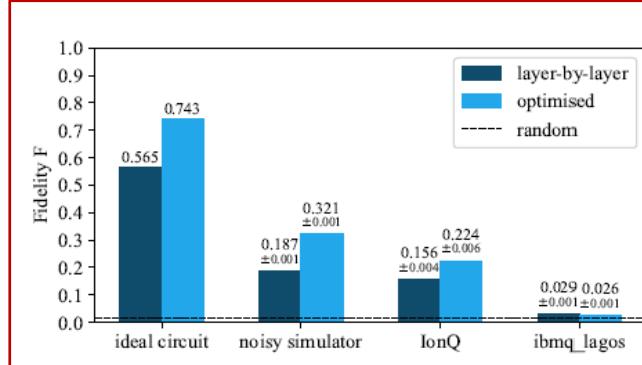


Bose-Einstein condensates



PRL 2022
Bar-Ilan Un

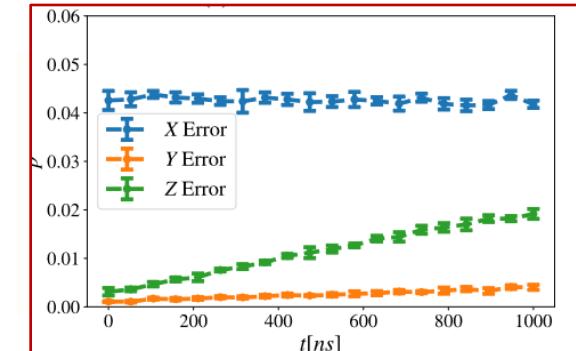
Quantum state encoding



arXiv



Quantum error detection



arXiv Emanuele Dalla Torre

smartArchive

NEW!

Personalized selection of daily preprints using AI



TRY IT FOR FREE

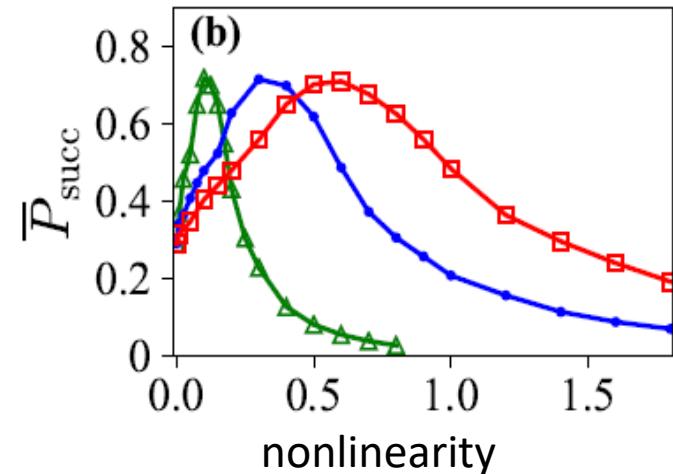
<http://tiny.cc/smarterArchive>



Summary: what did we learn?

Classical → energy-preserving coupling = limit cycles

L. Bello, M. Calvanese Strinati, EGDT, A. Pe'er, PRL&PRA (2020), NJP (2020)
M. Calvanese Strinati, L. Bello, EGDT, A. Pe'er, PRL (2021)

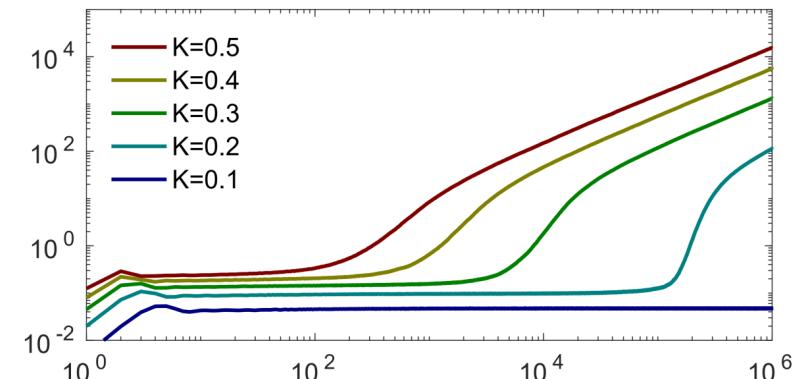


Many-body → statistical Floquet prethermalization $\frac{dE}{dt} \sim e^{-\frac{\Omega}{\Lambda}}$

Coupled Oscillators: Citro, Dalla Torre et al, Ann. of Phys., 2015
Rajak, Citro, Dalla Torre, JPA, 2018
Rajak, Dana, Dalla Torre, PRB (R), 2019
Saadia, EGDT, Rajak, PRR, 2019

Bose-Hubbard model: EGDT, Dentelski, Scipost 2021

Review: Wen Wei Ho, Takashi Mori, Dmitry Abanin, EGDT, arxiv 2022



Quantum → squeezing enhances coupling and dephasing

Theory: Inbar Shani, EGDT, Michael Stern, PRR 2021

Experiment: Villiers et al (Kondos&Leghtas group), arxiv

